

Grading for Integrated Algebra and Geometry

Homework

Oral Presentation

Quizzes

Problems of the week (POW)

Tests

Portfolio

Materials needed for Integrated Algebra and Geometry

1) Binder - 1-1/2 in

Pencil Case

2) Pencils

Book Socks

3) Lined Paper

4) 1/4 Inch Graph Paper

5) 12-inch Ruler with both Inch and Centimeter Scales

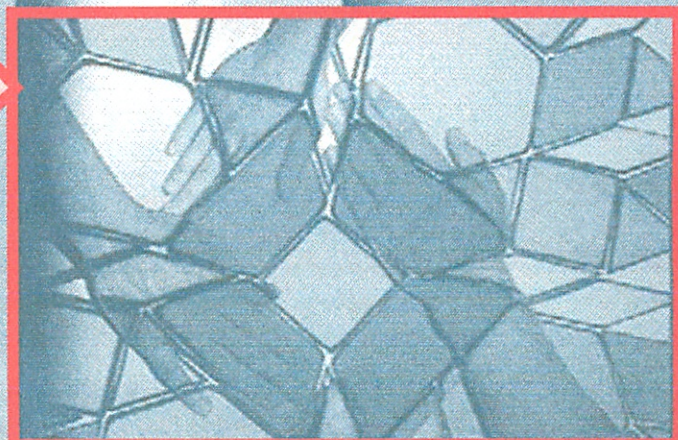
6) Colored Pencils

7) Protractor

8) Calculator (TI-83 PLUS)

Students do not need to bring their calculators to class, since graphing calculators will be provided. But they should have calculators available every night for use in the homework.

Patterns

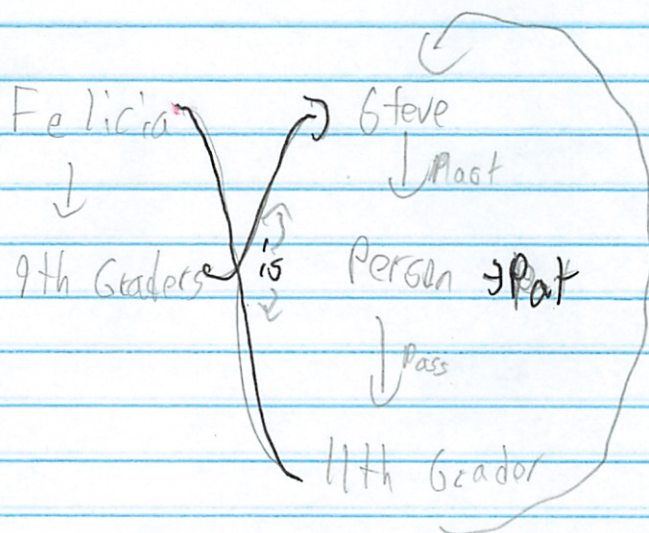


Who's Who (#2)

Michael Plomeier

9/9/04

Problem = ———
+ Work = ———

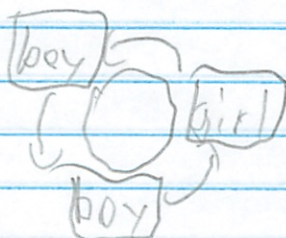


Process:

To solve this problem, I first put the facts in a diagram (above) I then looked at it to find a place with a — grader to a name as to match a name to a blank grader, as everyone has a name and grade. I then saw that Felicia could be the 9th grader, and Steve could be the 11th grader. The extra person must be Pat.

Solution: Steve / 9th Grade → Pat / 10th Grade → Felicia / 11th Grade

I know my solution is correct because all the people/grades are taken and the picture shows in order which looks like:



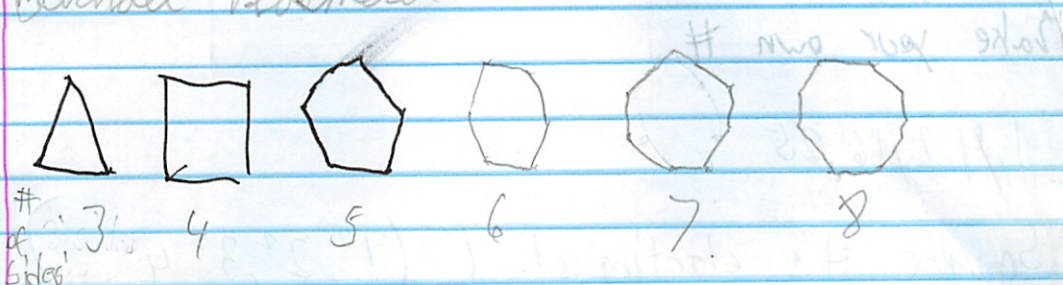
Describing Patterns

Michael Flemerier

9/9/04

key:

initial made up



2. 1, 1, 1, 2, 1, 3, 1, 4, 1, 5, 1, 6, 1, 7, 1, 8

1, a, 1, a+1, 1, a+1, 1

3. $\uparrow \downarrow \downarrow \uparrow \uparrow \uparrow \downarrow \downarrow \downarrow \downarrow \uparrow \uparrow \uparrow \uparrow \uparrow$ (down x 6) (up x 7)
 # of sides: UP down

$\uparrow = \text{odd}$ $\downarrow = \text{even}$

each time add 1 arrow, and alternate up/down

4. 1, 2, 4, 8, 16, 32

double the previous #

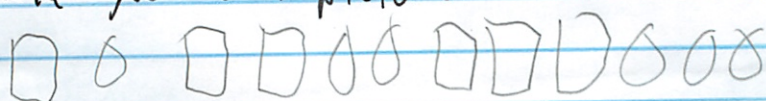
5. 1, 3, 5, 7, 5, 3, 1, 3, 5, 7, 5

Count odd # till 7, then odd # down to 1, repeat

6. 1, 3, 7, 15, 31, 63, 127, 255

Multiply previous # $\times 2$ and add 1

7. Make your own picture!



Do a square + circle, and add 1 of each, each time over

8. Make your own #.

1, 4, 9, 16, 25

Square #'s starting at 1 ($1^2, 2^2, 3^2, 4^2, \dots$)

Notes 1
 $-3^2 + (-3)^2$

9/9

The opposite of 3 to the 2nd power plus negative 3 to the 2nd power

My Way
 $-3^2 + (-3)^2$

His Way
 $-9 + 9$
 0

$-9 + 3^2$

$-9 + 9$

0

$-27 - (-1)^2 - (-2)^2 \div 8$

9/20

My Way

$-27 - 1 - 8 \div 8$
 $-27 - 1 - 8$

~~His Way~~

$(-1)^2 = -1 \times -1 = 1$
 (of)

$(-2)^2$

Powers x
Ways
 if Even its +
 if Odd its -

$(-2)^3 = -2 \times -2 \times -2$

His Way

$-27 - 1 + 8 \div 8$

$-27 - 1 + 1$

(-27)

PEMDAS

$-2^2 - 8 + (-3)^3 - 4 \div 2$

$-4 - 8 + -27 - 2$

$-10 + -29 = -39$

Over

$$-13 - 2$$

$$(-15) - (-41)$$

$$(-4)^3 + 3^2 - 2(3^2 - (-2)^3)^3$$

$$-64 + 9 - 2(9 - (-8))^3$$

$$-64 + 9 - 2(17)^3$$

$$-64 + 9 - 2(289)$$

$$-57 + 289$$

$$(98) 232$$

I_n	Out
2	5
3	8
4	11
5	14
6	17
9	26

Multiply by 3 + Subtract 1

$$I \times 3 - 1 = O$$

$$y = 3x - 1$$

$$y = \text{out} \quad x = \text{in}$$

Graphing for
Slope

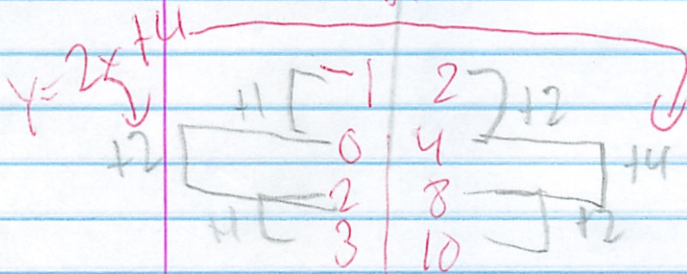
p2

in	out
0	4
2	8
-1	2
3	10

Multiply by 2 + Add 4

~~Add 2~~ Square it
 $y = 2x + 4$

Put it in order



In	Out
0	1
1	2
2	5
5	26

Not good

$m = y^2 + 1$ quadratic equation

$y = \text{in}$
 $m = \text{out}$

! = factorial

$$2! = 2 \times 1$$

$$8! = 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 = 40,320$$

Michael Plasmeier

9/12/2004

P.D.:

POW Beginnings

HW # 4

1. *1. Problem Statement:* The problem in this POW is that there are eggs, that only fit in groups [boxes] of 7. When places in groups of 2, 3, 4, 5, 6, there is 1 egg left over. You need to find out how many eggs there are.

2. The answer is not correct, because 49 divided by 4 gives you a remainder of 1, not 4.

Test	2	3	4	5	6	7
49 48 r1	16 r1	12 r1	9 r4	8 r1		7

Trial of 100 49

Inside Out (#5)

Michael Plasmeier

9/13

1.

In	Out
2	4
3	6
11	22
27	54
9	18

~~Weed~~
~~an~~
~~an~~
~~an~~

2.

In	Out
2	7
9	13
7	22
10	31
12	37
25	76

$x = in$
 $y = out$
for all

$y = 3x + 1$

"The Out is
double the In"
 $y = x2$

"The Out is 1 plus
triple the In"

3.

In	Out
house	4
cup	2
Writer	5
elephant	7
Spin	3
mathematics	10
plug	3
paragraph	8
a	0

$x + 1 = x$

"The In is a word
with 1 less number
than the out"

4.

In	Out
0	3
1	11
2	15
3	7

"The Out is 4x
the # of eyes
minus 1"

$y = 4x - 1$

Rules for Back

45 6. "The Out is equal to 2 times the In plus 5" $y = 2x + 5$
70 7. "The Out is the factorial of the # of stars" $y = x!$ Over

5.	In	Out
	division	I
	ever	F
	opportunity	O
	toast	A
	safe	F
	people	O
	mathematics	F
	<u>the</u>	(can't be done)

"The Out. is the 2nd vowel in the In." *capitalized*

6.	In	Out
	0	5
	3	11
	10	25
	7	19
	28	

In	Out
5	x
6	10
7	12
9	16
12	22
$y = 2(x - 1)$	
$y = x + (x * 2)$	
$y = 2x - 2$	
In	Out
6	5
18	9
9	6
12	7
15	
12	12

7.	In	Out
	x x x	6
	x x	7
	x x x y x	128
	x x x x y	

In	Out
10	7
4	4
5	4.5
15	9.5
20	12
18	11
6	5
18	9
9	6
12	7
15	
12	12

In	Out
18	81
12	36
9	20.25
16	4
21	100

$$y = (x \div 2)^2$$

In	Out
1	3
3	8
4	26
6	772
$y = x \div 2 + 2$	
$y = \frac{x}{2} + 2$	
In	Out
2	837
3	1257
8	3329
	4877098

$$x! + 12 = y$$

In	Out
2	837
3	1257
8	3329
	4877098

$$y = 415x + 7$$

Constants
Coefficients Variables

Notes p3

9/13

Expressions - no =

Equation - have =

Independent variable

	P	x
2p	3	6
	5	10
	8	16

Dependent variables

factor - division
distributive multiplication

$$3(x+2)$$

distributing
properties

3x + 6 multiply each

$$4x^2 - 8x$$

$$4x(x-2)$$

factoring

9/17

In	Out
0	0
1	22
2	44
3	66
4	88
5	110
6	132
7	154

x by 22

$$y = 22x$$

In	Out
0	2
1	3
2	6
3	11

$$y = x^2 + 2$$

might help

$$x^2 = 9$$

$$x = 3 \text{ or } -3$$

IMP

Worksheet

1

Getting to 1 (#6)

Michael Plasmeyer

4/14

1. a. 6, 3, 10, 5, 16, 8, 4, 2, 1
 b. 9, 28, 14, 7, 22, 11, 34, 17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1
 c. 21, 64, 22, 11, 34, 17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1
 d. 33, 100, 50, 25, 76, 38, 19, 58, 29, 88, 44, 22, 11, 34, 17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1

2. a. ~~8~~ (8) b. 20 (19) c. 18 (17) d. 27 (26) ^{Count} Don't First 1.

3. 3 | 8, 4, 2, 1
 4 | 16, 8, 4, 2, 1
 5 | 5, 16, 8, 4, 2, 1

4. You could work backwards by multiplying by 2 or 2^{100} or pick a very high odd #.

5. The pattern always jumps onto a track at 16, but prior to that

Pow

#1

Marcella's Bagels

9/15

Store

Check ~~44~~ 88

Half +2

$$22 - 2 = 20 \quad 44 - 2 = 42$$

Half +2

$$10 - 2 = 8 \quad 22 - 2 = 20$$

Half +2

$$4 - 2 = 2$$

Home

2

②

$$(2 + 2) \times 2 = (8 + 2) \times 2 = (20 + 2) \times 2 = 44 \text{ At the Store}$$

Start

#7

Worksheet 2

Michael Plasmier

9/17

$$1. (8+3) \times 2^3$$

$$11 \times 8$$

$$(88)$$

$$2. 54 - 2 \times 3^3 + 4^3$$

$$54 - 2 \times 27 + 64$$

$$54 - 54 + 64$$

$$0 + 64$$

$$(64)$$

$$3. 15 - 9 \div 3 + 6 \times 2$$

$$15 - 3 + 12$$

$$12 + 12$$

$$(24)$$

$$4. 12 + 12 \div 12$$

$$12 + 1$$

$$(13)$$

$$5. 4 \times 9 - 6 \div 3 + 1$$

$$36 - 2 + 1$$

$$34 + 1$$

$$(35)$$

$$6. 14 \times [12 \div (3 \times 3 \times 3)]$$

$$14 \times [12 \div (3 \times 9)]$$

$$14 \times [12 \div 27]$$

$$14 \times 1$$

$$(14)$$

$$7. 9^2 + 2^3 \times 5$$

$$49 + 8 \times 5$$

$$49 + 40$$

$$(89)$$

$$8. 4 \times (9 - 6) \div 2 + 4 = 10$$

$$9. (6+3) \times 4+3 + (2^3 \times 2) - 7 = 48$$

Don't Need

$$10. (10 - 4 + 3) \times 4 + 5 \times 2 = 46$$

Name Michael Plasmeier

Date 9/17/04

Perform the order of operations to solve each of the following.

1) $(8 + 3) \cdot 2^3 =$ 55

2) $54 - 2 \cdot 3^3 + 4^3 =$

3) $15 - 9 \div 3 + 6 \cdot 2 =$

4) $12 + 12 \div 12 =$

5) $4 \cdot 9 - 6 \div 3 + 1 =$

6) $14 \cdot [12 \div (3 + 3 \cdot 3)] =$ _____

7) $92 + 2^3 \cdot 5 =$ _____

Insert the **fewest sets of parentheses** that will make each of the following true.

8) $4 \cdot 9 - 6 \div 2 + 4 = 10$

9) $6 + 3 \cdot 4 + 3 + 2^3 \cdot 2 - 7 = 48$

10) $10 - 4 + 3 \cdot 4 + 5 \cdot 2 = 46$

Notes

9/28

a. $\frac{8!}{(6-2)! \times 2!}$

$$\frac{30240}{24 \times 2}$$

$$\frac{30240}{48}$$

$$\begin{array}{r} 42 \\ 8 \times 7 \times 6 \times 5 \\ 252 \\ 1260 \end{array}$$

$$\begin{array}{r} 24 \\ 5 \overline{) 1260} \\ 5840 \end{array}$$

$$\begin{array}{r} \times 3 \\ 15120 \\ 30240 \end{array}$$

$$48 \overline{) 30240}$$

b. $\frac{6!}{4-3! \times 2!}$

$$\frac{720}{1 \times 2}$$

$$\frac{720}{2}$$

$$(360)$$

$$6 \times 5 \times 4$$

$$\begin{array}{r} 120 \\ \times 3 \\ 360 \end{array}$$

$$720$$

this way

$$\begin{array}{l} 4 + \\ 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 \\ \times 4 \times 3 \times 2 \times 1 \end{array}$$

do this to get answer

$$\sqrt{4} = 2 = (\text{?} \times \text{?} = 4)$$

9/21

$$\sqrt[3]{8} = (\text{?} \times \text{?} \times \text{?} = 8) \div 2 = \text{The cubed root of 8}$$

$$\sqrt[4]{8} = x \times x \times x \times x = 8 \div 2 = \text{The fourth root of 8}$$

$$x^3 = x \times x \times x$$

Uncertain Ans. (7/9)

9/21

1. $(12 - 8) \times (1 + 7) = 32$

- 2. $8 - (15 + 6) \div 3 = 1$

- 3. $(7 + 3)^2 = 100$

4. $(24 + 16) \div (8 - 4) = 10$

5. $20 \div (7 - 2) + 5^2 \times 3 = 79$

6. $7 - 5 \times 8 + 6 \div 2$
 $7 - 40 + 3 = -36$

7. $2 \times 8 + 3 = 19$
 $2 \times 14 \div 2 = 14$

7. $4 + 9 - 6 \div 2 \times 5 + 1$
 $4 + 9 - 3 \times 5 + 1 = -1$
 ~~$13 - 6 \div 2 \times 5 + 1 = -1$~~
 $4 + 9 - 6 \div 2 \times 6 = 31$
 $4 + 3 \div 2 \times 5 + 1 = 12.5$

NAME: Michael Plasméia IMP I

DATE: 9/21

a) Complete the In-Out table

$y = 4x - 7$
Out = $4 \cdot \text{In} - 7$

In	Out
.6	-5.4 -4.6
4	17.9 9
$2\frac{3}{5}$	14.4 32
$2\frac{1}{6}$	-6.2 -5.8
.3	12.2 4.8

Handwritten notes: 2.4, 2.6, 7.0, 1.4, 1.2, 7.0 not, 4.8, 19.2

a) Complete the In-Out table

Out = $\text{In} - 4$
 $y = x - 4$

In	Out
2	-2 -2
-5	-9 -9
$3\frac{1}{4}$	-2.25 $or -\frac{3}{4}$
5.7	1.7 1.7
-8	-12 -12

Handwritten notes: 16 2/3

a) Complete the In-Out table

Out = $2\frac{1}{5} \cdot \text{In} + 1$

In	Out
0	1 1
$1\frac{1}{2}$	1.5 $1\frac{1}{5}$
$2\frac{2}{3}$	1.4 $1\frac{4}{5}$
$3\frac{1}{4}$	1.3 $1\frac{3}{5}$
$5\frac{3}{5}$	7.2 $7\frac{2}{5}$
$5\frac{1}{16}$	1.1 $1\frac{1}{8}$

Handwritten notes: 1 8/5 3/10, 2 2/5 4/5, 3 3/5 5/5, 2 3/5 20, 2 3/5 28, 3 2/5 5, 5 8/5 7, 2 3/5 21

a) Complete the In-Out table

Out = $4 \cdot \text{In} - 3$
 $y = 4x - 3$

In	Out
.9	.6 3.6
$3\frac{1}{4}$	18 $13\frac{1}{4}$
.25	-2 9.75
$11\frac{1}{2}$	3 57
9	36 33

Handwritten notes: 3, Had it

a) Complete the In-Out table

Out = $13 - 4 \cdot \text{In}$
 $y = 13 - 4x$

In	Out
-2	-8 21
-3	-27 25
$-\frac{7}{9}$	-7 $11\frac{1}{9}$
$5\frac{1}{4}$	12.25 $12\frac{1}{4}$
.25	12.25 $12\frac{1}{4}$

Handwritten notes: 16 x 1st not 14.16

a) Complete the In-Out table

Out = $5 \cdot \text{In} + \frac{1}{3}$

In	Out
.2	1.3 $1\frac{1}{3}$
$2\frac{2}{3}$	3.3 $3\frac{5}{3}$
$7\frac{1}{10}$	3.5 $3\frac{5}{10}$
0	1/3 $1\frac{1}{3}$
$1\frac{1}{5}$	1.3 $1\frac{1}{5}$

Handwritten notes: 2 5/3 11/3, 6 1/3 17/3, 7 1/2 6 1/2, 2 3/5 35/5

a) Complete the In-Out table

Out = $2 \cdot \text{In} + 1$

In	Out
5	11 11
-3	-5 -5
$2\frac{1}{2}$	6 6
-2.7	-4.4 -4.4
8	17 17

Handwritten notes: 2.7, 3.4, 3.8

a) Complete the In-Out table

Out = $2 \cdot \text{In} - 3$

In	Out
.2	-1 -1
.5	-1.7 -1.7
2.3	4.3 4.3
3.5	7.3 7.3
4.6	8.9 8.9
5.7	11.4 11.4

Handwritten notes: 11.1

Out = $2 \cdot \text{In} - 3$

In	Out
.2	2.6 2.6
.5	-2 -2
2.3	1.6 1.6
5.15	7.3 7.3
4.6	6.2 6.2
5.7	9.4 9.4

Quiz

9/22

Notes

9/23

1, 2, 3, 4, 5, 6, ...

Counting or Natural Numbers

0, 1, 2, 3, 4, 5, 6

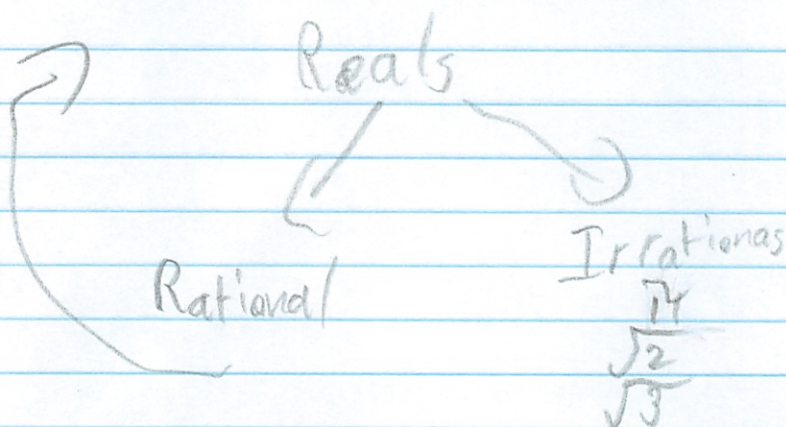
Whole #s

-5, -4, -3, -2, -1, 0, 1, 2, 3

Integers

Reals

Decimals → ^{terminate}
 ^{repeat}
 could be fractions



Consecutive up Sums

9/23

$$1+2=2$$

$$2+3=5$$

$$3+4=7$$

$$4+5=9$$

$$5+6=11$$

Add
2

$$1+2+3=6$$

$$4+5+6=15$$

$$7+8+9=24$$

$$10+11+12=33$$

+9

$$\begin{aligned} 1+2+3 &= 6 \\ 3+4+5 &= 12 \\ 5+6+7 &= 18 \\ 7+8+9 &= 24 \end{aligned} \quad \begin{aligned} &+4 \\ &+4 \\ &+4 \\ &+4 \end{aligned}$$

$$\begin{aligned} 1+2+3+4 &= 10 \\ 5+6+7+8 &= 26 \\ 9+10+11+12 &= 42 \end{aligned} \quad \begin{aligned} &+6 \\ &+16 \\ &+16 \end{aligned}$$

$$1+2=3$$

$$1+2=3$$

$$3+3=6$$

$$9+4=13$$

$$13+5=18$$

$$18+6=24$$

$$24+7=31$$

$$31+8=39$$

Goes up

$$1+2+3+4+5=15$$

$$2+3+4+5+6=20$$

$$3+4+5+6+7=25$$

$$4+5+6+7+8=30$$

+5

$$10+11+12=33$$

$$30+33+36=99$$

$$60+66+72=198$$

+3

+2

Not consecutive

Act the same

Not consecutive

$$\begin{aligned} &1+2+3+4+5=15 \\ &10+11+12+13+14+15=75 \\ &20+21+22+23+24+25=135 \\ &30+31+32+33+34+35=195 \end{aligned} \quad \begin{aligned} &+60 \\ &+60 \\ &+60 \\ &+60 \end{aligned}$$

When you add 2 numbers next to each other. (Each 1 is a problem x2) you add 2, however if you don't use a # 2x, then it goes up 4. When you add 3#, (each one 1x) then the difference goes up 1, but then 4# the difference goes up 16.

When you add 5# [5x] then it goes up 5. When you add x each 1st place x10, then the answer goes up 66.

His Answers

9/24

Any odd number can be found using consecutive sums of 2

ex: $13 = 6 + 7$

$$51 = 25 + 26$$

$$201 = 100 + 101$$

Except 1

Any 3rd sequence is middle $\# \times 3$

$$2 + 3 + 4 = 9 = 3 \times 3$$

$$5 + 6 + 7 = 18 = 6 \times 3$$

$$8 + 9 + 10 = 27 = 9 \times 3$$

$$11 + 12 + 13 = 36 = 12 \times 3$$

1st
+ 6th

Notes

Σ = Significance + Summation

$\sum_{x=1}^5 x$ The sum of all the x from 1 to 5

$$1 + 2 + 3 + 4 + 5 = 15$$

$$\sum_{x=0}^3 2x^2 = 2(0)^2 + 2(1)^2 + 2(2)^2 + 2(3)^2 = 28$$

The sum of all the $2x^2$ from 0 to 3

Hw

#10

Name Michael Plasencia
 Date 9/24

Patterns Unit
 In/Out tables #2

Complete the In-Out tables.

1) Out = $3 \cdot \text{In} + 7$

IN	OUT
0.6	<u>8.8</u>
4	<u>19</u>
$2\frac{3}{5}$	<u>14.8</u> $\frac{13}{5} \cdot \frac{3}{1} \frac{39}{5} 7.8$
0.3	<u>7.9</u>
<u>1.73</u>	<u>12.2</u>
or $\frac{11}{15}$	

2) Out = $\text{In}^2 - 4$

IN	OUT
2	<u>0</u>
-5	<u>-29</u> 21
$3\frac{1}{4}$	<u>5.8</u> $6\frac{4}{16}$
5.7	<u>28.41</u> $5.7 \cdot 5.7 = 32.49$
	<u>-12</u>
	<u>-8</u>

No answer

3) Out = $\frac{2}{5} \cdot \text{In} - 1$

IN	OUT
0	<u>-1</u>
$\frac{1}{5}$	<u>-1.4</u> $\frac{1}{2} \cdot \frac{2}{5} \frac{1}{5}$
$\frac{2}{5}$	<u>-1.2</u> $\frac{2}{3} \cdot \frac{2}{5} \frac{4}{15}$
$\frac{3}{5}$	<u>-1</u> $7\frac{2}{3}$
$\frac{5}{16}$	<u>-1.25</u> $\frac{5}{8} \cdot \frac{2}{4} \frac{1}{8}$

4) Out = $4 \cdot \text{In} + 3$

IN	OUT
0.9	<u>3.36</u> 6.69
$\frac{3}{4}$	<u>6</u> 6.75 $\frac{3}{4} \cdot 4 \frac{3}{1}$
4	<u>19</u>
0.25	<u>4</u>
$1\frac{1}{2}$	<u>7</u> $\frac{3}{2} \cdot 4 \frac{5}{1}$
<u>1.5</u>	<u>9</u>

5) Out = $3 \cdot \text{In}$

IN	OUT
-2	<u>-6</u>
-3	<u>-9</u>
$-2\frac{1}{3}$	<u>-7</u>
$\frac{5}{4}$	<u>$3\frac{3}{4}$</u> $\frac{5}{4} \cdot 3 \frac{15}{4} 3\frac{3}{4}$
$\frac{4}{5}$	<u>1.2</u>
0.25	<u>0.75</u>

6) Out = $3 \cdot \text{In} + \frac{1}{3}$

IN	OUT
0.2	<u>1.1</u>
$\frac{2}{3}$	<u>2</u> $\frac{2}{3} \cdot 3 \frac{2}{3}$
$\frac{7}{10}$	<u>2.1</u> $\frac{7}{10} \cdot 3 \frac{21}{10}$
10	<u>30.33</u>
$\frac{1}{5}$	<u>0.6</u> $\frac{1}{5} \cdot 3 \frac{3}{5}$

7) Out = $3 \cdot \text{In} - 1$

IN	OUT
5	<u>14</u>
-3	<u>-10</u>
$2\frac{1}{2}$	<u>6.5</u> $\frac{5}{2} \cdot 3 \frac{15}{2}$
-2.7	<u>-7.1</u> -1.91
<u>5.3</u>	<u>17</u>

8) Out = $\text{In} \div 3$

IN	OUT
0.2	<u>$\frac{1}{15}$</u> $\frac{2}{30} = \frac{1}{15}$
0.5	<u>$\frac{1}{6}$</u> $\frac{5}{30} = \frac{1}{6}$
2.3	<u>$\frac{23}{30}$</u> $\frac{23}{30}$
5.7	<u>1.9</u> $\frac{57}{30}$

State the rule for each In-Out table.

9) RULE:

$y = x \cdot 3 + 1$

IN	OUT
6	17
4	11
11	32
9	26
1	2
24	71
16	47

$3 \overline{) 46}$

10) Rule:

Letter after

In	Out
CHP	DIQ
IMT	JNU
WED	XFE
BUN	CVO
HOG	IPH
YET	2 F U
E K X	FLY

11) Rule:

~~$y = x^3$~~

In	Out
11	484
2	16
5	100
8	256
9	324
10	1000 400
11	144

$y = (2x)^2$

$y = 4x^2$

12) RULE:

$y = x^3$

IN	OUT
-3	-9
5	15
$3\frac{2}{3}$	11
-2.4	-7.2
15	45

Pow #2

Pattern

Qv2 9/24

Notes

$$\sum_{x=2}^5 2x$$

The sum of all the $2x$'s from $x=2$ to 5.

2(2) + 2(3) + 2(4) + 2(5)
 4 + 6 + 8 + 10
 (28)

$$\sum_{w=3}^6 (w-1)^2$$

The sum of $(w-1)^2$ from $w=3$ to 6

$$(3-1)^2 + (4-1)^2 + (5-1)^2 + (6-1)^2$$

$$2^2 + 3^2 + 4^2 + 5^2$$

$$4 + 9 + 16 + 25$$

$$54$$

Write this in
sigma

$$4 + 5 + 6 + 7 + 8$$

$$\sum_{x=4}^8 x$$

$$\sum_{x=4}^8 x$$

$$\sum_{x=0}^4 (x+4)$$

11

Practice

T_n	Out
-1	-7
2	2
1	-1 $\times 3 - 4$
0	-4
n	$3n - 4$
$5\frac{1}{2}$	12
	16

The Out is 3 times the T_n minus 4

H/W
9/29

$$1. \sum_{x=3}^9 x = 3 + 4 + 5 + 6 + 7 + 8 + 9 = (42)$$

9/29

$$2. \sum_{w=3}^8 (w^2 + 2) = 3^2 + 2 + 4^2 + 2 + 5^2 + 2 + 6^2 + 2 + 7^2 + 2 + 8^2 + 2$$

$$9 + 2 + 16 + 2 + 25 + 2 + 36 + 2 + 49 + 2 + 64 + 2$$

$$11 + 18 + 27 + 38 + 51 + 66$$

$$(211)$$

3. Write:

$$\frac{4}{2} + \frac{4}{4} + \frac{4}{6} + \frac{4}{8}$$

$$2 + 1 + \frac{2}{3} + \frac{1}{2}$$

$$3 + \frac{7}{6}$$

$$(4\frac{1}{6})$$

$$\sum_{x=1}^8 \left(\frac{4}{x+x} \right) =$$

#12

Cubes p39

Do it the Chef's Way (#13)

9/30

1. a $-3 + 5 = +2$
- b $5 - 4 = +9$
- c $(2 \times 6) = -12$
- d $-(4 \times 7) = -28$
- e $-(3 \times -6) = +18$

- 2a Add 4 hot cubes and take away 4 cold cubes $= 7^\circ$
- b Add 6 cold cubes and 4 cold cubes $= -10^\circ$
- c Take away 10 bunches of 5 cold cubes $= -50^\circ$
- d Add 4 groups of 8 cold cubes $= -32^\circ$

- HW
- #13 1 Add 6 cold cubes and 9 cold cubes $= +15^\circ$
 - 4 Add 4 cold cubes and take away 6 hot cubes $= -10^\circ$
 - 7 Take away 3 groups of 4 cold cubes $= -12^\circ$
 - 2 Add 7 cold cubes and take away 10 cold cubes $= -3^\circ$
 - 5 Add 3 hot cubes and Add 7 cold cubes $= -4^\circ$
 - 8 Add 8 hot cubes and take away 12 cold cubes $= 20^\circ$
 - 3 Add 5 bunches of 2 cold cubes $= -10^\circ$
 - 6 Take Away 6 bunches of 9 hot cubes $= -54^\circ$
 - 9 Add 12 cold cubes and 5 hot cubes $= -7^\circ$

Write out each of these summation problems as a string of numbers added together and find the sum.

1) $\sum_{x=1}^5 (2x) =$

2) $\sum_{k=1}^5 6 =$

3) $\sum_{v=0}^3 (3v-1) =$

4) $\sum_{r=0}^3 r^2 =$

5) $\sum_{k=0}^4 9k =$

6) $\sum_{k=0}^3 \frac{1}{k^2+1} =$

7) $\sum_{t=2}^7 (5t)^2 =$

8) $\sum_{x=2}^6 (x+2)(x-3) =$

Use the summation notation to write the given sums.

9) $\frac{5}{1+1} + \frac{5}{1+2} + \frac{5}{1+3} + \dots + \frac{5}{1+15} =$ *Means Solve it*

10) $4(1) + 4(2) + 4(3) + \dots + 4(9) =$

11) $1 + 3 + 5 + 7 + 9 =$

12) $2 + 2 + 2 + 2 + 2 =$

$$1. \quad \begin{array}{cccccc} 2 \times 1 & + & 2 \times 2 & + & 2 \times 3 & + & 2 \times 4 & + & 2 \times 5 \\ 2 & & 4 & & 6 & & 8 & & 10 \end{array}$$

(30)

$$2. \quad 6 + 6 + 6 + 6 + 6$$

(30)

$$3. \quad \begin{array}{ccccccc} 3 \times 0 - 1 & + & 3 \times 1 - 1 & + & 2 \times 3 - 1 & + & 3 \times 3 - 1 \\ 0 - 1 & + & 3 - 1 & + & 6 - 1 & + & 9 - 1 \end{array}$$

(14)

$$4. \quad 0^2 + 1^2 + 2^2 + 3^2$$

(14)

$$5. \quad \begin{array}{cccccc} 9 \times 0 & + & 4 \times 1 & + & 9 \times 2 & + & 9 \times 3 & + & 9 \times 4 \\ 0 & + & 9 & + & 18 & + & 27 & + & 36 \end{array}$$

(90)

$$6. \quad \frac{1}{0^2+1} + \frac{1}{1^2+1} + \frac{1}{2^2+1} + \frac{1}{3^2+1}$$

$$\frac{1}{1} + \frac{1}{2} + \frac{1}{5} + \frac{1}{10}$$

(1 $\frac{8}{10}$) or $\frac{14}{5}$

$$7. \quad (5 \times 2)^2 + (5 \times 3)^2 + (5 \times 4)^2 + (5 \times 5)^2 + (5 \times 6)^2 + (5 \times 7)^2$$

$$100 + 225 + 400 + 625 + 900 + 1225$$

$$8. \quad \begin{array}{ccccccc} (2+2) \times (2-3) & + & (3+2) \times (3-3) & + & (4+2) \times (4-3) & + & (5+2) \times (5-3) \\ 1-4 & & 1 & & 1 & & 14 \end{array}$$

$$16 + (6+2) \times (6-3)$$

$$16 + 24$$

Answer $\rightarrow$

9. $\sum_{x=1}^{15} \left(\frac{8}{1+x} \right)$

10. $\sum_{x=1}^9 4(x) = 180$

11. $\sum_{x=1}^5 2x - 1$

12. $\sum_{x=1}^5 2 = 10$

Solve them
too

Warm up

The sum of ~~4~~ from 1 to 5

~~X~~ $\sum_{x=1}^5 4 = \text{can't be done } 4+4+4+4+4$ 20

$\sum_{x=0}^3 8 = 8+8+8+8 = \text{32}$
 $x=0 \text{ counts}$

(2) $\sum_{x=1}^3 (x+1)^3 = (1+1)^3 + (2+1)^3 + (3+1)^3$

$\begin{array}{r} 2 \\ 16 \\ + 27 \\ + 64 \\ \hline 107 \end{array}$

3. $\frac{4}{1} + \frac{4}{3} + \frac{4}{5} + \frac{4}{7} = \sum_{x=1}^7 \frac{4}{x^2} = \frac{4}{1^2} + \frac{4}{3^2} + \frac{4}{5^2} + \frac{4}{7^2} + \frac{4}{9^2} + \frac{4}{11^2} + \frac{4}{13^2}$

$\begin{array}{r} 64 \\ 27 \\ + 8 \\ \hline 99 \end{array}$
 $\frac{4}{x^2} - 1$
 $\frac{4}{1^2} - 1 = 3$
 $\frac{4}{3^2} - 1 = \frac{4}{9} - 1 = -\frac{5}{9}$
 $\frac{4}{5^2} - 1 = \frac{4}{25} - 1 = -\frac{21}{25}$
 $\frac{4}{7^2} - 1 = \frac{4}{49} - 1 = -\frac{45}{49}$
 $\frac{4}{9^2} - 1 = \frac{4}{81} - 1 = -\frac{77}{81}$
 $\frac{4}{11^2} - 1 = \frac{4}{121} - 1 = -\frac{117}{121}$
 $\frac{4}{13^2} - 1 = \frac{4}{169} - 1 = -\frac{165}{169}$

Write Up

$\sum_{x=2}^6 x^2 + 3$

$7 + 12 + 19 + 28 + 39$
 $\begin{array}{ccccccc} & 15 & 17 & 19 & 21 & 23 & 25 \\ & \swarrow & \downarrow & \swarrow & \downarrow & \swarrow & \downarrow \\ & 15 & 17 & 19 & 21 & 23 & 25 \end{array}$
 each +2

not same means its powers

Michael Plasencia

Sigma Notation 1

Write out each of these summations problems as a string of numbers added together and find the given sum.

1. $\sum_{i=1}^5 (2i) =$

5. $\sum_{k=1}^5 6k =$

~~2. $\sum_{i=0}^3 (3i \pm 1) = 3 \cdot 0 + 1 + 3 \cdot 1 + 1 + 3 \cdot 2 + 1 + 3 \cdot 3 + 1 = 6 + 1 + 3 + 1 + 6 + 1 + 9 + 1 = 30$~~

6. $\sum_{i=0}^4 i^2 =$

3. $\sum_{k=1}^4 9 =$

7. $\sum_{k=0}^2 \frac{1}{k^2 + 1} =$

4. $\sum_{n=2}^6 (5n)^2 =$

8. $\sum_{k=2}^5 (k+1)(k \pm 3) =$

Do All
or Both

Use the summation notation to write the given sums.

9. $\frac{5}{1+1} + \frac{5}{1+2} + \frac{5}{1+3} + \dots + \frac{5}{1+15} =$

11. $1+3+5+7+9 =$

10. $4(1) + 4(2) + 4(3) + \dots + 4(9) =$

12. $2+2+2+2 =$

Sigma Notation 2

Write out each of these summations problems as a string of numbers added together and find the given sum.

1. $\sum_{i=1}^4 (3i) =$

5. $\sum_{k=3}^6 5k =$

2. $\sum_{i=0}^3 (5i + 2) =$

6. $\sum_{i=1}^4 i^3 =$

3. $\sum_{k=1}^4 3 =$

7. $\sum_{k=1}^3 \frac{1}{k^2 + 3} =$

4. $\sum_{n=2}^5 (3n)^2 =$

8. $\sum_{k=2}^5 (k+2)(k+1) =$
 $(2+2) \times (2+1) + (3+2) \times (3+1) + (4+2) \times (4+1) + (5+2) \times (5+1)$
 $4 \times 3 + 5 \times 4 + 6 \times 5 + 7 \times 6$
 $12 + 20 + 30 + 42$
 104

Use the summation notation to write the given sums.

9. $\frac{2}{3+1} + \frac{2}{3+2} + \frac{2}{3+3} + \dots + \frac{2}{3+15} =$

11. $2 + 4 + 6 + 8 + 10 =$

10. $5(3) + 5(4) + 5(5) + \dots + 5(9) =$

12. $7 + 7 + 7 + 7 =$

Side 1

10/4

1. $2 \cdot 1 + 2 \cdot 2 + 2 \cdot 3 + 2 \cdot 4 + 2 \cdot 5$
 $2 + 4 + 6 + 8 + 10$
 (30)

3. $9 + 9 + 9 + 9$
 (36)

4. $(5 \cdot 2)^2 + (5 \cdot 3)^2 + (5 \cdot 4)^2 + (5 \cdot 5)^2 + (5 \cdot 6)^2$
 $10^2 + 15^2 + 20^2 + 25^2 + 30^2$
 $100 + 225 + 400 + 625 + 900$
 (2250)

5. $6 \cdot 1 + 6 \cdot 2 + 6 \cdot 3 + 6 \cdot 4 + 6 \cdot 5$
 $6 + 12 + 18 + 24 + 30$

6. $0^2 + 1^2 + 2^2 + 3^2 + 4^2$
 $0 + 1 + 4 + 9 + 16$
 (30)

7. $\frac{1}{0^2+1} + \frac{1}{1^2+1} + \frac{1}{2^2+1}$
 $\frac{1}{1} + \frac{1}{2} + \frac{1}{5}$
 $(\frac{7}{10})$

9. $\sum_{x=1}^{15} \frac{5}{1+x} = \frac{5}{1+1} + \frac{5}{1+2} + \frac{5}{1+3} + \frac{5}{1+4} + \frac{5}{1+5} + \frac{5}{1+6} + \frac{5}{1+7} + \frac{5}{1+8} + \frac{5}{1+9} + \frac{5}{1+10} + \frac{5}{1+11} + \frac{5}{1+12} + \frac{5}{1+13} + \frac{5}{1+14} + \frac{5}{1+15}$
 $\frac{5}{2} + \frac{5}{3} + \frac{5}{4} + \frac{5}{5} + \frac{5}{6} + \frac{5}{7} + \frac{5}{8} + \frac{5}{9} + \frac{5}{10} + \frac{5}{11} + \frac{5}{12} + \frac{5}{13} + \frac{5}{14} + \frac{5}{15}$

10. $\sum_{x=1}^9 4x = 4 \cdot 1 + 4 \cdot 2 + 4 \cdot 3 + 4 \cdot 4 + 4 \cdot 5 + 4 \cdot 6 + 4 \cdot 7 + 4 \cdot 8 + 4 \cdot 9$
 $4 + 8 + 12 + 16 + 20 + 24 + 28 + 32 + 36$
 (180)

Over

11.

$$\sum_{x=1}^5 2x-1 = (1 \cdot 2 - 1) + (2 \cdot 2 - 1) + (3 \cdot 2 - 1) + (4 \cdot 2 - 1) + (5 \cdot 2 - 1)$$

$$2 \cdot 1 + 4 \cdot 1 + 6 \cdot 1 + 8 \cdot 1 + 10 \cdot 1$$

$$1 + 3 + 5 + 7 + 9$$

$$(25)$$

$$12. \sum_{x=1}^5 2 = 2 + 2 + 2 + 2 + 2$$

$$(10)$$

Side 2

$$1. (3 \times 1) + (3 \times 2) + (3 \times 3) + (3 \times 4)$$

$$3 + 6 + 9 + 12$$

$$(30)$$

$$2. (5 \cdot 0 + 7) + (5 \cdot 1 + 2) + (5 \cdot 2 + 7) + (5 \cdot 3 + 2)$$

$$0 + 2 + 5 + 2 + 10 + 2 + 15 + 2$$

$$(38)$$

$$3. 3 + 3 + 3 + 3$$

$$(12)$$

$$4. (3 \times 2)^2 + (3 \times 3)^2 + (3 \times 4)^2 + (3 \times 5)^2$$

$$6^2 + 9^2 + 12^2 + 15^2$$

$$36 + 27 + 144 + 225$$

$$(432)$$

$$5. 5 \times 3 + 5 \times 4 + 5 \times 5 + 5 \times 6$$

$$15 + 20 + 25 + 30$$

$$(90)$$

$$6. 1^3 + 2^3 + 3^3 + 4^3$$

$$1 + 8 + 27 + 64$$

$$(100)$$

$$\begin{array}{r} 48 \\ + 12 \\ \hline 96 \\ + 560 \\ \hline 656 \end{array}$$

$$7. \frac{1}{1^2+3} + \frac{1}{2^2+3} + \frac{1}{3^2+3}$$

$$\frac{1}{4} + \frac{1}{7} + \frac{1}{12} = \frac{10}{21}$$

$$12. \sum_{x=1}^4 7 = 7 + 7 + 7 + 7$$

$$(28)$$

$$9. \sum_{x=1}^{15} \frac{2}{3+x} = \frac{2}{3+1} + \frac{2}{3+2} + \frac{2}{3+3} + \frac{2}{3+4} + \frac{2}{3+5} + \frac{2}{3+6} + \frac{2}{3+7} + \frac{2}{3+8} + \frac{2}{3+9} + \frac{2}{3+10} + \frac{2}{3+11} + \frac{2}{3+12} + \frac{2}{3+13} + \frac{2}{3+14} + \frac{2}{3+15}$$

$$\frac{1}{2} + \frac{2}{5} + \frac{2}{6} + \frac{2}{7} + \frac{2}{8} + \frac{2}{9} + \frac{2}{10} + \frac{2}{11} + \frac{2}{12} + \frac{2}{13} + \frac{2}{14} + \frac{2}{15}$$

$$(3.322.548.49)$$

$$10. \sum_{x=3}^9 5x = 5 \times 3 + 5 \times 4 + 5 \times 5 + 5 \times 6 + 5 \times 7 + 5 \times 8 + 5 \times 9$$

$$15 + 20 + 25 + 30 + 35 + 40 + 45$$

$$(210)$$

$$\sum_{x=1}^5 2x = 2 + 4 + 6 + 8 + 10$$

$$(30)$$

Michael Plummer

Perform the following operations.

1. $4 - 3 + 1$
1+1

2. $24 \div 2 \cdot 3$
12 x 3

3. $4 - 3 - 1$
1-1

4. $14 - 8 + 3 - 1$
6+3-1

5. $(5 - 2) \cdot 3^2$
3 x 9

6. $9 - (4 - 2)^2$
1-2^2
9-4

7. $14 - 2 \cdot 5 - 3$
14-10-3

8. $24 \cdot 4 \div 2$
96 ÷ 2

9. $18 - 3^2$
18-9

10. $28 - 2 \cdot 3^2 + 3^2$
28-2x9+9
28-18+9

11. $(21 - (16 - (5 - 3)))$
21-16-2

12. $15 - 9 + 5 - 3 + 1$
6+5-3+1
11-3+1

13. $72 \div 9 \div 4 \div 2$
8 ÷ 4 ÷ 2
2 ÷ 2

14. $4 \cdot 9 - 5 - 3 + 1$
36-5-3+1

15. $(12 - 3^2) - 4^2 \div 2$
12-9-16 ÷ 2
3^2-8
9-8

1. 2

2. 24

3. 8

4. 8

5. 27

6. 5

7. 1

8. 48

9. 9

10. 19

11. 3

12. 9

13. 1

14. 29

15. 1

Perform the following operations.

1. $8 - 3 + 1$
 $5 + 1$

2. $28 \div 7 \cdot 2$
 4×2

3. $8 - 6 \div 2$
 $8 - 3$

4. $18 - 8 + 3 - 1$
 $10 + 3 - 1$

5. $5 + 2 \cdot 3^2$
 $5 + 2 \cdot 9$
 $5 + 18$

6. $9 - (5 - 2)^2$
 $9 - 3^2$
 $9 - 9$

7. $18 - 2 \cdot 5 + 3$
 $18 - 10 + 3$

8. $9 \cdot 8 \div 2$
 $72 \div 2$

9. $3(5 - 3)^2$
 $3 \cdot 2^2$
 $3 \cdot 4$

10. $36 \div 4 \cdot 3^2 + 3^2$
 $9 \cdot 9 + 9$

11. $(25 - (23 - (5 - 3)))$
 $25 - 23 - 2$

12. $25 - 9 + 5 - 3 + 1$
 $16 + 5 - 3 + 1$
 $21 - 3 + 1$

13. $128 \div 8 \div 4 \div 2$
 $16 \div 4 \div 2$
 $4 \div 2$

14. $8 \cdot 9 - 5 - 3 + 1$
 $72 - 5 - 3 + 1$
 $67 - 5 - 3 + 1$

15. $(15 - 3)^2 - 4^2 \div 2$
 $(15 - 9)^2 - 16 \div 2$
 $6^2 - 8$
 $36 - 8$

1. 6

2. 12

3. 5

4. 12

5. 23

6. 0

7. 12

8. 36

9. 12

10. 90

11. 0

12. 19

13. 2

14. 60

15. 28

Perform the indicated operation(s). Simplify the answer.

1. $-3 + 5 = 2$
2. $6 - 9 = -3$
3. $-7 \cdot 8 = -47$
4. $4 + (-3) = 1$
5. $9 + (-4) = 5$
6. $1 + (-6) = -5$
7. $3 \cdot (-5) = -15$
8. $-5 + 7 = 2$
9. $-2 + (-5) = -7$
10. $-3 \cdot (-4) = 12$
11. $-6 - 7 = -13$
12. $-6 \div (-3) = 2$
13. $-4 + (-1) = -5$
14. $8 \div (-2) = -4$
15. $3 - 5 = -2$
16. $-5 + 2 = -3$
17. $-4 \div (-8) = 0.5$
18. $-2 + 8 = 6$
19. $-2 \cdot 8 = -16$
20. $-6 + 3 = -3$
21. $-2 + 6 - 3 = 1$
22. $-7 - 5 - 3 = -15$
23. $5 - 2 - 7 + 3 = -1$
24. $-3 \cdot 2 \cdot (-3) = 18$
25. $-2 + 3 + 4 - 5 = 0$
26. $-4 + (-3) + (-2) - 1 = -10$
27. $6 - 7 - 7 - 4 = -12$
28. $4 \cdot (-3) \cdot (-2) = 24$
29. $-2 \cdot (-3) \cdot (-2) \cdot (-2) = 24$
30. $-3 + (+3) + (+3) = 3$
31. $-2 \cdot 5 \cdot (-3) \cdot (-2) = -60$
32. $6 + (+1) + (-5) \div (-4) = 6.25$
33. $-2 \cdot (-3) = 6$
34. $-7 + (-4) - (-9) = -2$
35. $-24 \div (-4) \div (-2) = -3$
36. $-9 - 8 - 7 - 6 = -30$
37. $-3 \cdot 4 \cdot (-2) = 24$
38. $2 + (-3) + 2 + (-5) = -4$
39. $4 - (+3) + 5 + (-7) = 5$
40. $3 \cdot (-2) \cdot 5 \cdot (-3) = 90$

Perform the indicated operation(s). Simplify the answer.

1. $-13 + 5 = -8$

2. $4 - 9 = -5$

3. $-7 - 8 = -15$

4. $-4 + (-3) = -7$

5. $9 - (-4) = 13$

6. $16 + (-1) = 15$

7. $3 + (-5) = -2$

8. $-5 - 7 = -12$

9. $-5 + (-3) = -8$

10. $-3 + (-4) = -7$

11. $-8 - (-7) = -1$

12. $-6 + (-3) = -9$

13. $-4 + (-1) = -5$

14. $8 - (-2) = 10$

15. $-3 + 5 - (-4) = 6$

16. $-5 + 2 - 5 = -8$

17. $-4 + (-8) - 3 = -15$

18. $-2 + 8 + (-4) = 2$

2 -'s make (+)
1 -'s make (-)

Perform the indicated operation(s). Simplify the answer.

1. $-3 \cdot 5 = -15$

2. $6(-9) = -54$

3. $-7 \cdot 8 = -56$

4. $-4 \cdot (-3) = 12$

5. $16 \div (-4) = -4$

6. $21 \div (-6) = -3.5$

7. $3 \cdot (-5) = -15$

8. $-5 \div 15 = -\frac{1}{3}$

9. $-2 \cdot (-5) = 10$

10. $-3 \cdot (-4) = 12$

11. $\frac{-24}{-6} = 4$

12. $-6 \div (-3) = 2$

13. $-\left(\frac{32}{-4}\right) = 8$

14. $8 \div (-2) = -4$

15. $\frac{45}{-3} = -15$

16. $-\left(\frac{-12}{-3}\right) = -4$

17. $-4 \div (-8) = .5$

18. $-12 \div 8 = -1.5$

Notes

10/11

You can collect like terms

$$6 - (-1) + (-5) - (-4)$$

$$\rightarrow 6 + 1 - 5 + 4$$

$$\downarrow$$

$$11 - 5$$

$$\rightarrow 6$$

10/11

1. $-3 + -4 = -7$ - take away 3 hot cubes and add 4 cold cubes
2. Add 4 hot cubes and take away 8 cubes
 $+4 - (-8) = 12$
3. $-6 \times 3 = -18$ - Take away 6 groups of 3 hot cubes
4. $3 \times -5 = -15$ - Add 3 groups of 5 cold cubes
5. $-3 + -4 = (-8)$ - Take away 3 hot cubes and add 4 cold cubes. Then take away 8 cold cubes



Absolute value - the distance from 0

$$\text{Symbol} = |2|$$

Example

$$|-3| = |3| = 3 \quad | -4 | = 4 \quad -|4| = -4$$

over $\rightarrow$

$$\frac{||4-8|| - |4-5|}{4-8}$$

$$\frac{||4-1|| - |1-1|}{-4} = \frac{4-1}{-4} = \frac{3}{-4} = \left(-\frac{3}{4}\right)$$

$$\left. \begin{array}{l} (2.1)^2 \\ 21^2 \\ 4.41 \end{array} \right\}$$

Perfect²
to 25

10/11

1	1
2	4
3	9
4	16
5	25
6	36
7	49
8	64
9	81
10	100
11	121
12	144
13	169
14	196
15	225
16	256
17	289
18	324
19	361
20	400
21	441
22	484
23	529
24	576
25	625

Big jump
small jump

Patterns

Qv2

10/6

Rules, Rules, Rules (#15)

10/11

1. Rules: $y = x + 11$ $y = (x + 11)$
 $\checkmark y = 3x + 1$ $y = 4x - 4$
 $y = (x + 3) \cdot 2$ $y = (x + 27) \div 2$
 $y = 20x - 84$ $y = 6x \div 2 + 1$
 $y = 0x + 16$
 $y = 2x + 6$

2. ~~$y = 2x + 1$~~
 $y = 3x - 1$ $y = 4x - (x + 1)$
 $y = x^2 + 1$ $y = 4x - x - 1$
 $y = (x + 1) / 3 - 4$ $3x$
 $y = x + 1$

Another In-Outer (#16)

10/11

1. To get the out the 1st letter is size, 2nd is color, 3rd is shape

$\square = LWS$

2. $\Delta = LWT$

2. $y = -3x$ $13 = -39$ $-7 = 21$ $10 = -30$ ~~$-11 \frac{2}{3}$~~ ~~-35~~

3. $y = 3x + 2$ $-5 = -13$ $0 = 2$ $-7 = -19$

4. ~~Last letter + 8 down alpha?~~ The out = the next letter of the alph of the 3rd letter
 Robert = ~~B~~ C

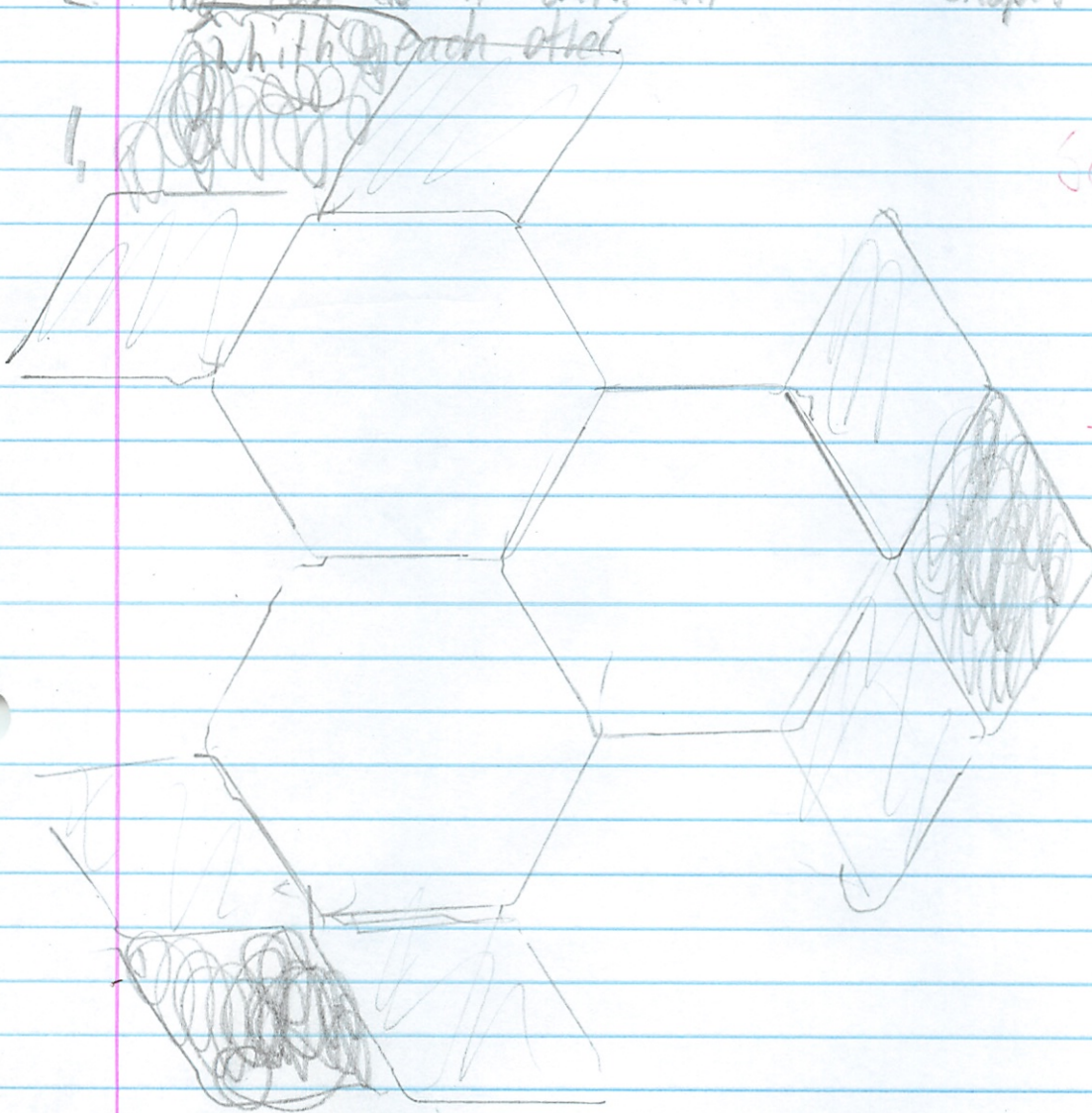
5. ~~add this~~
 $\text{hair} = 5$, $\text{eyes} = -2$ $y = (\text{hair})^2 + (\text{eyes})$
 last one = 21 27

6. $y = -3x + 1$ $3 = -8$ $-2 = 7$ $-3 = 10$

Pattern Block

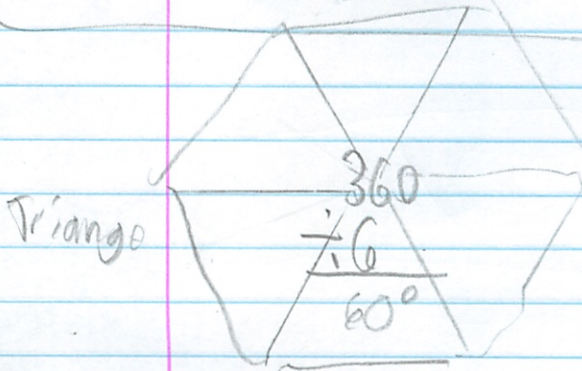
p43

2. You can do it with all of the shapes together
 1. ~~with each other~~



See Angle
Notes

p46



$$\Diamond = 360^\circ / 360^\circ = 120^\circ \text{ each for big side}$$

2 smalls are 120°
 1 small is 60°

More

Notes

10/13

$+7$ = Positive seven

-7 = negative seven

Sign - indicates whether the number is positive or negative

Zero - neither positive nor negative

$+3$ and -3 are opposites

Integer - a number that is either zero, a natural number or the opposite of a natural number

Greater than: $>$

Less than: $<$

Absolute value - the distance a number is from 0

$$|5| = 5 \quad |-7| = 7$$

Polygon: A closed two-dimensional shape formed by 3 or more line segments

Triangle: A polygon w/ 3 sides.

Quadrilateral: A 4 sided figure

Square: A 4 sided polygon w/ all sides of equal length
4 right angles

Rhombus: A 4 sided polygon whose sides are all sides
Pair same length

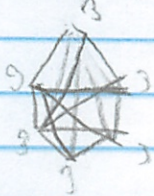
Trapezoid: 4 sided polygon w/ 1 pair of parallel sides

Michael Plasma'ia

Diagonally Speaking #17

10/13

1.

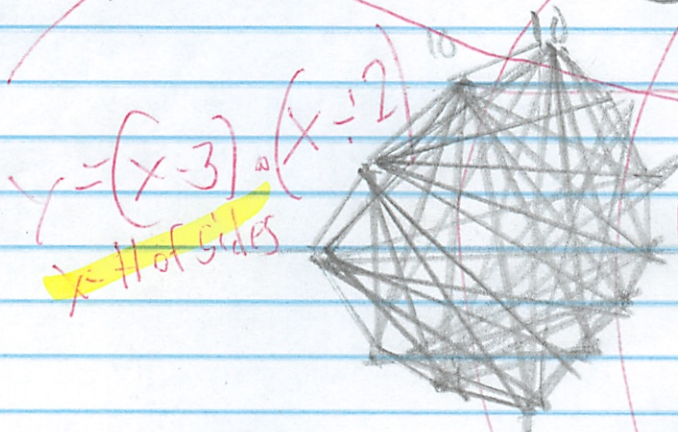


In # of sides	Out # of diagonals
3	0
4	2
5	5
6	9
7	14
8	20
9	27
10	35

2.

Add up the number of vertices and subtract 2, by half, then multiply that # by the number of vertices and cut that in half.

$$12 - 2 = 10 \times 12 = 120 / 60$$



$$x^2 - 3x$$

3.

This pattern holds because each vertex is connected to diagonal points, except for the 2 on the side of the shape. They are a certain number of points/vertices they all have same # of diagonals. Because a diagonal has 2 vertices divide that # in half, that is your answer.

Michael Plasmeier

A Protracted Engagement



Deon and Marsha thought of an interesting way to announce their long-awaited wedding.

They decided to send the invitations out in code. In the code they decided on, each letter is represented by an angle of a certain size.

An angle between 0° and 5° represents the letter A, an angle between 5° and 10° represents B, an angle between 10° and 15° represents C, and so on.

To avoid confusion, they never used angles that were exact multiples of 5° . The design below spells out part of their invitation.

>	A
5	A
10	B
15	C
20	D
25	E
30	F
35	G
40	H
45	I
50	J
55	K
60	L
65	M
70	N
75	O
80	P
85	Q
90	R
95	S
100	T

① What does this message say? *Please Come*

2. Make up a message of your own that is between 10 and 20 letters long. You and other students can exchange and decipher each other's messages.

TA6

1

Triangle Notes

10/14

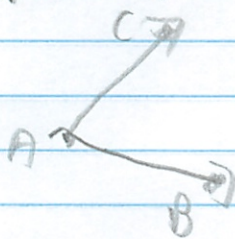
One complete turn has 360°

Degree: name for a turn for $\frac{1}{360}$ of a complete turn

Right Angle: an angle with a measure of 90°

Acute Angle: an angle whose measure is between 0° and 90°

Obtuse Angles: angle whose measure is between 90° and 180°



Vertex: Point A is the vertex of this angle

Sides of the angle are ray AB and ray AC

Name the angle using all 3 points with the vertex in the middle. Our angle is angle BAC or angle CAB

Ray: The part of a line from a single point, called the vertex, through another point on the line, continuing infinitely in that direction.

Degree Discovery

+ Polygon Angles (#18)

	1	2	3	Average
Triangle	179	181	180	180°
Quad.	345	351	358	354
5-Gon	543	442	449	478
Hexagon	497	624	554	558

of side polygons in

in	out
3	180
4	360
5	540
6	720
7	900

sum of angles

Measure of each

sides and angles are same

angle of a

regular n-gon

3	60
4	90
5	108
6	120
7	128 4/7

n. $(n-2) \times 180$

Triangle Conclusion: The Triangles add up to 180° and when you put 3 angles together they make a line.

Squares should equal 360° It equals 354°

5-Gon - Have very different results. 2 are similar. No pattern.

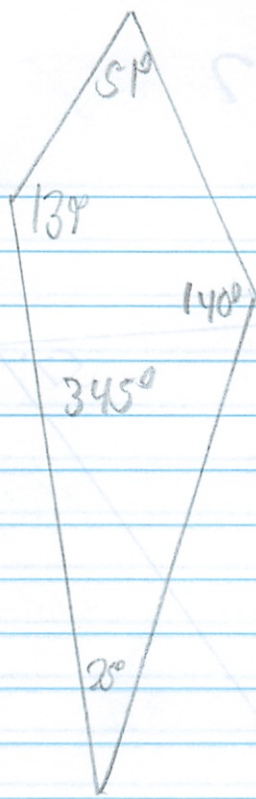
Hexagon - Answer far apart, though average is close to shape 3.

#18

Total - There is no pattern I found, although the average increase does go down.

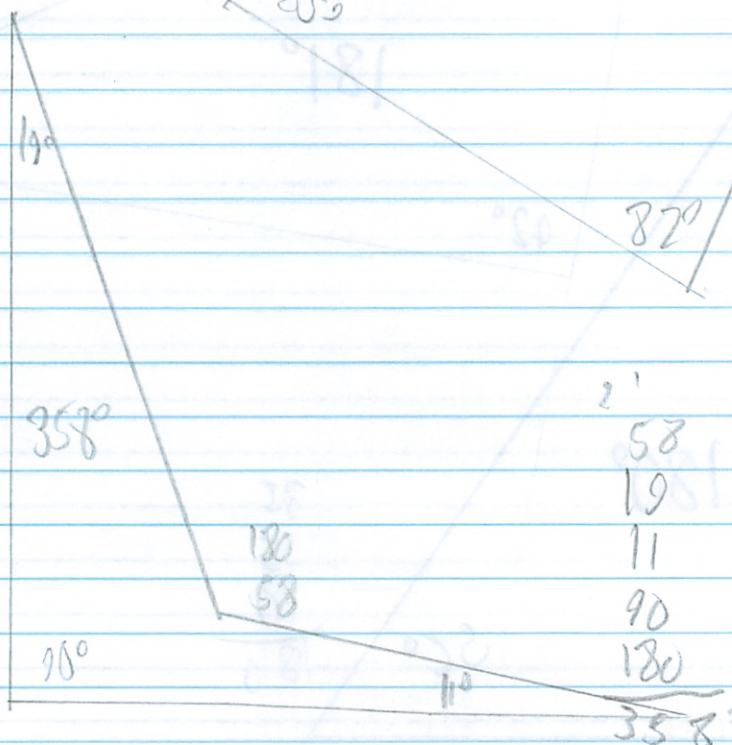
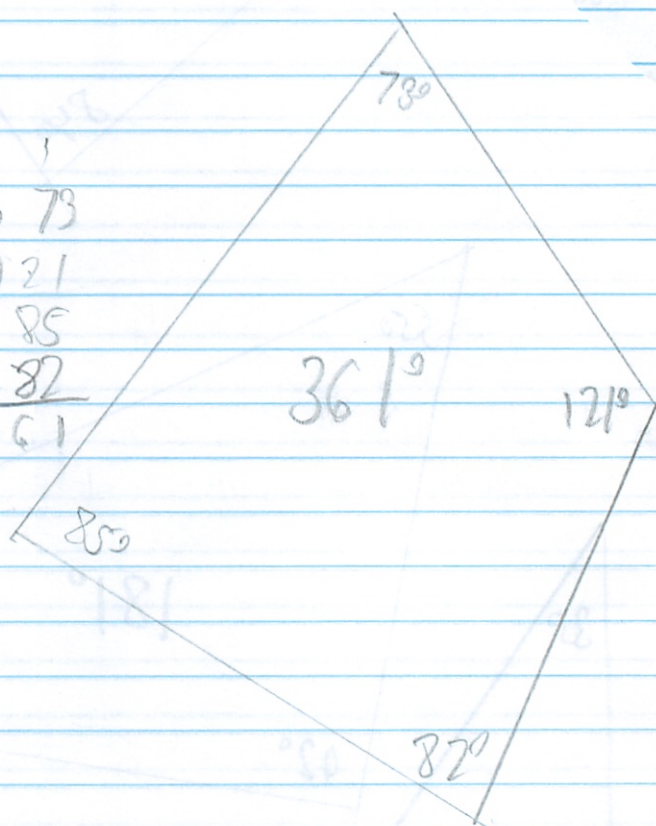
I can't make any generalization, although the more sides, the bigger the sum of the angles.

Multiply # of sides (subtract 2) by 180



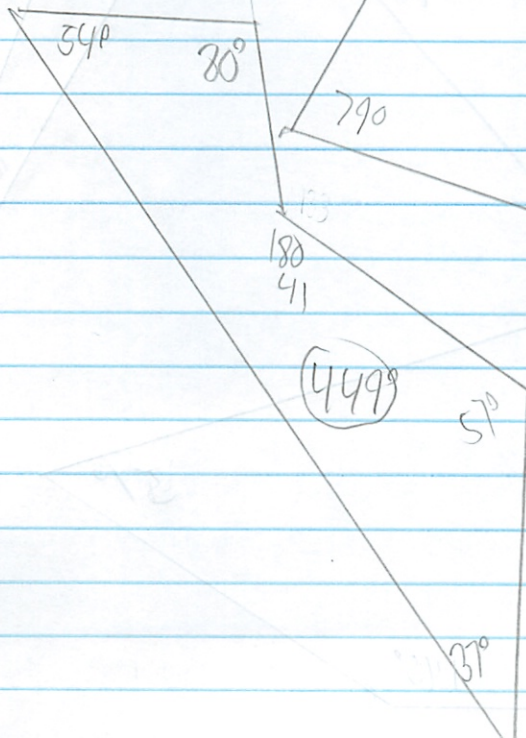
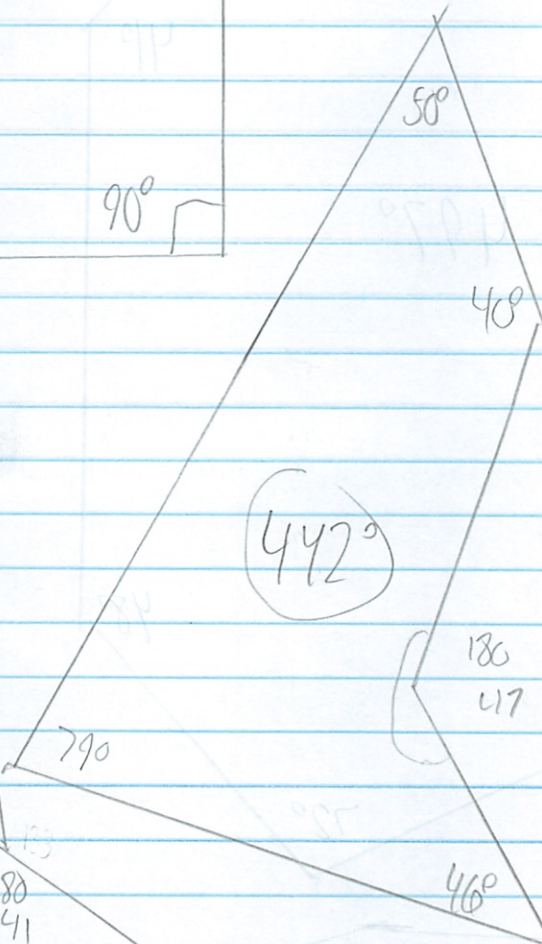
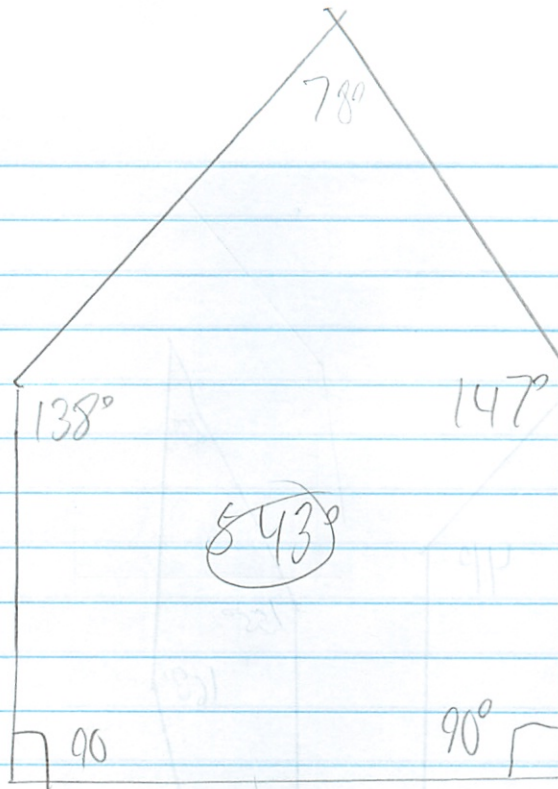
$$\begin{array}{r} 25 \\ 140 \\ 51 \\ \hline 139 \\ 345 \end{array}$$

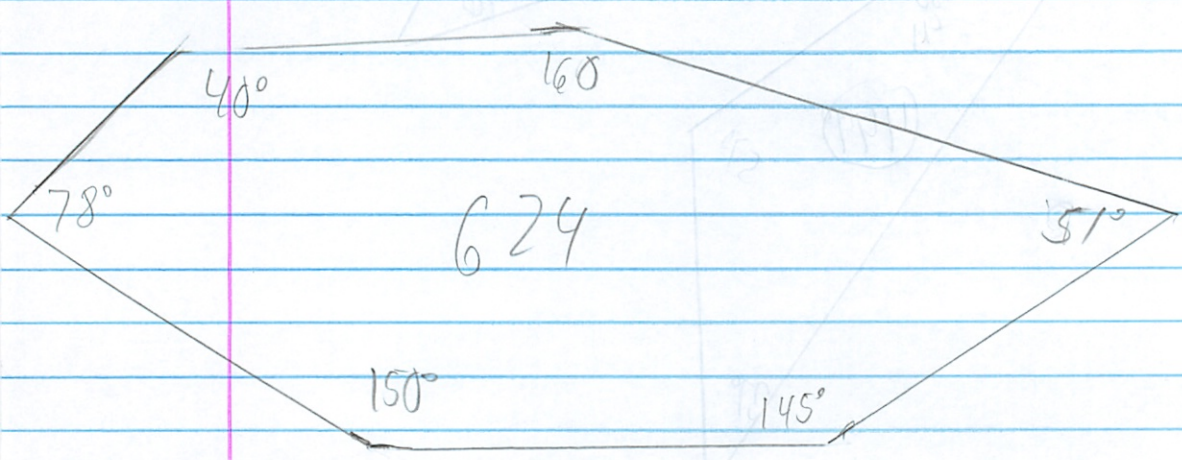
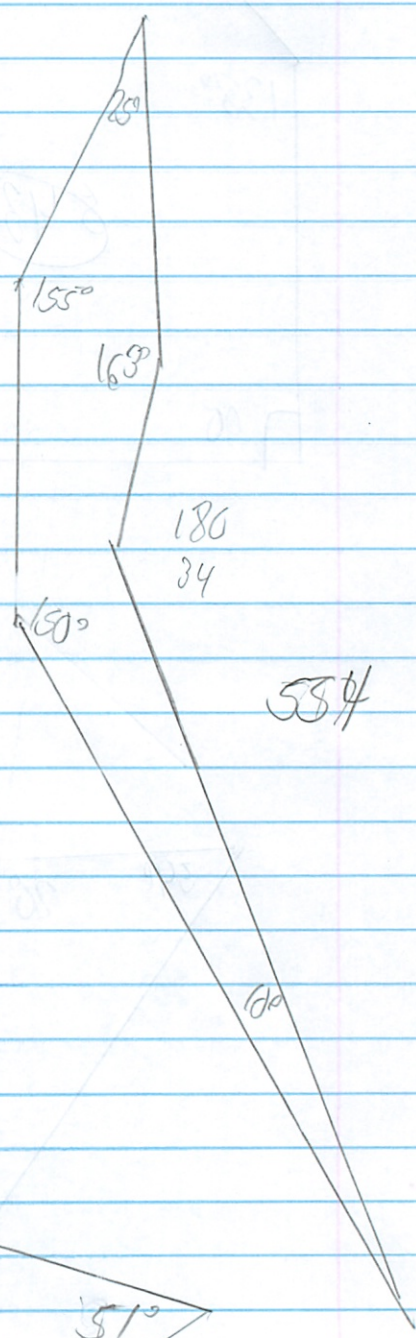
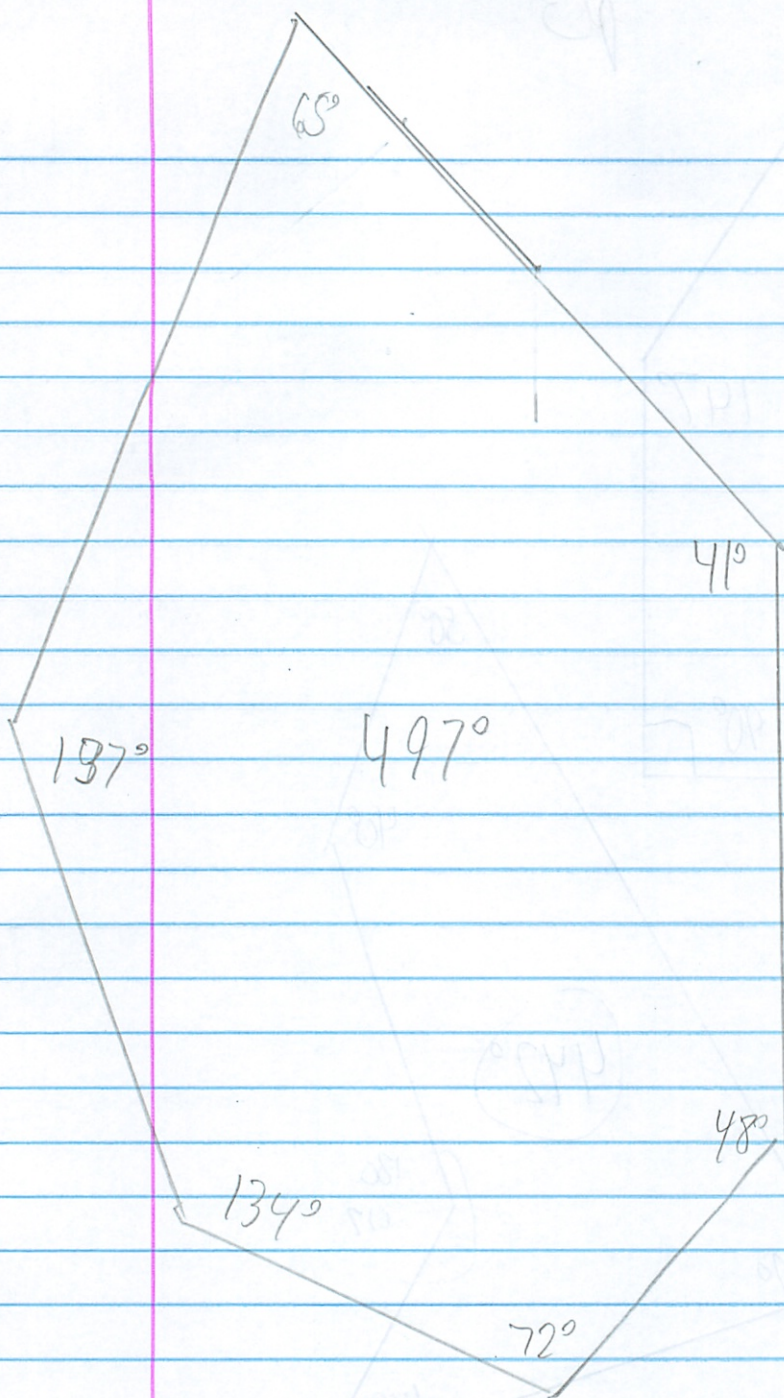
$$\begin{array}{r} 1 \\ 73 \\ 121 \\ 85 \\ \hline 82 \\ 361 \end{array}$$



$$\begin{array}{r} 2 \\ 58 \\ 19 \\ 11 \\ 90 \\ 180 \\ \hline 358 \end{array}$$

p3





Angles Notes

10/15

The angle of a polygon is an angle formed when 2 sides of the polygon meet at a vertex

Recursive function is a rule that tells how to get a value out from the previous out value

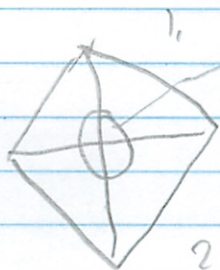
All Regular Polygon

Color of (Figure)	Figure
Green (Equilateral triangle)	60°
Yellow (Hexagon)	120°
Orange (square)	90°
Brown (Small Rhombus)	30° and 150°
Blue (Rhombus)	60° and 120°
Red (Trapezoid)	60° and 120°

Regular Polygon - a polygon that has all of its sides equal and all of its angles are =

Proof gone bad

10/15



He is adding these angles, which are not the side

2. Just take those out.

Real #

Quiz

10/13

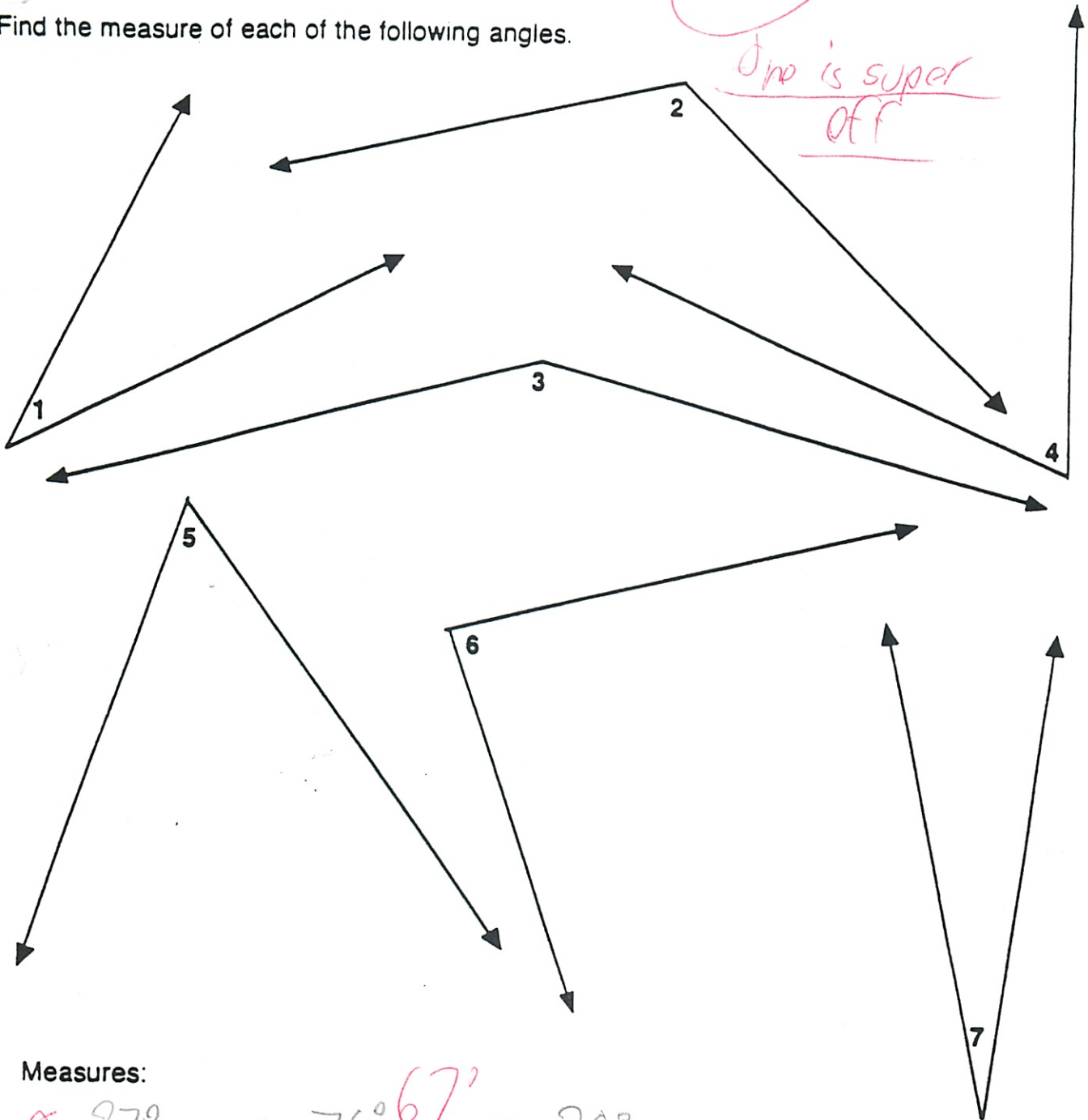
Patterns Pop

Quiz 10/13

Name: Michael Plasencia

PATTERNS DAY 17

Find the measure of each of the following angles.



Measures:

$\angle 1$ 87°
 $\angle 2$ 122.5°
 $\angle 3$ 151°
 $\angle 4$ 76°
 $\angle 5$ 56°
 $\angle 6$ 84.5°
 $\angle 7$ 20°

Sauces and Scoops (#20)

10/16

1.

Height (h)	# Sauces (x)
1	1
2	3
3	6
4	10
5	15
6	21
7	28
8	36
9	45
10	55
10	828

$(x/2)(x-1) + x$
 Distributing $\frac{x^2}{2} - \frac{x}{2} + 1$
 Recursive Formula $\frac{x^2}{2} + \frac{x}{2}$
 $\frac{x+1}{2} \times x$
 $x \rightarrow n = (\text{new})x \cdot \frac{x^2 + x}{2}$
 Or add all the ns above including 1st
 $3 = 3 + 2 + 1 = 6$

$\sum_{x=1}^n x$ ✓ $\frac{x+1}{2} \times x$

2.

# Scoops (n)	Ardago (x)
1	1
2	2
3	6
4	24
5	120
6	
7	
10	

a. 3

1	1	2	2	3	3
2	3	3	1	1	2
3	2	1	3	2	1

1	2	3
2	3	4
3	4	5

6	3	1
3	3	2
1	2	1

b. Formula

$x = n!$

forgot something

5040
3,102,880

It's like probability from last year

c. 100!

Garden Border #21

in Class

#22

10/18

~~x = number of rows~~
~~n = length of 1 side~~
~~x = # of savers~~

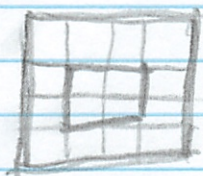
36

1. $4n - 4 = x$  - 4

2. $2n + 2(n-2) = x$ 

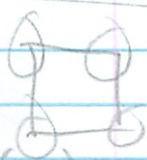
3. $4(n-1) = x$ 

4. $n^2 - (n-2)^2$



= total area
 - minus inside

#22

1. a. $2s + 2(s-2)$  b. $s + 2(s-1) + (s-2)$  c. $4(s-2) + 4$ 

2. $s^2 - (s-2)^2$  

2. $s + s + s + s - 4$



10
 10
 10
 10
 40
 sides
 don't count corners 2x

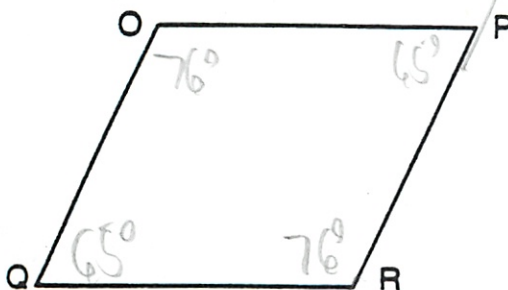
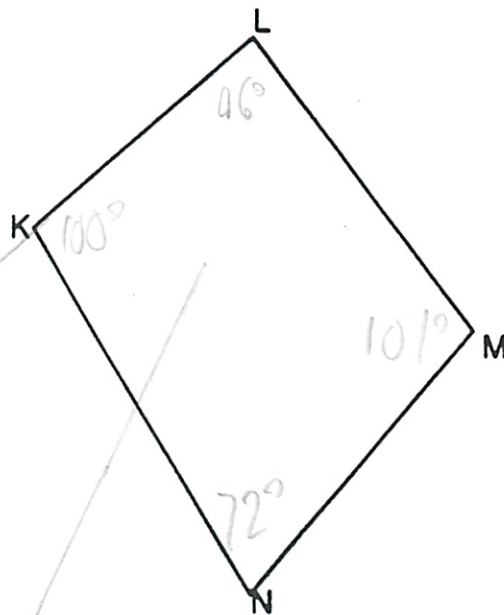
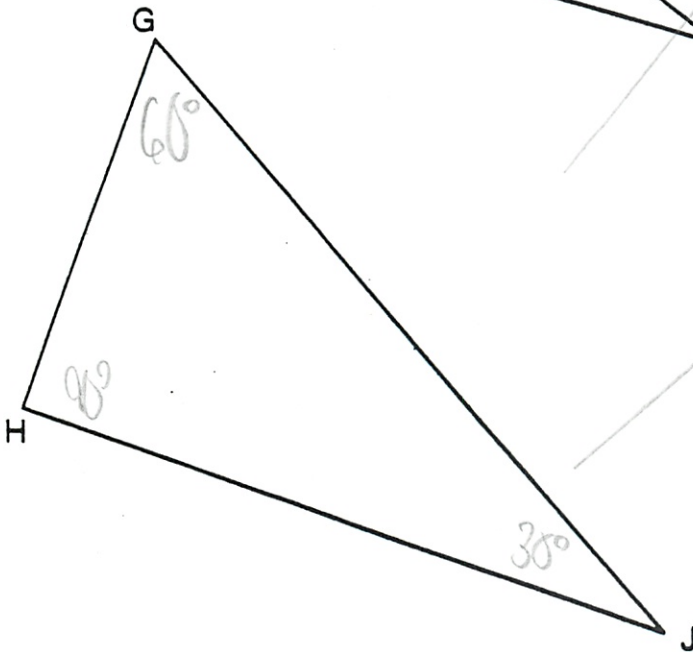
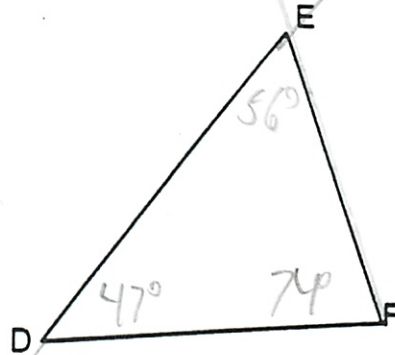
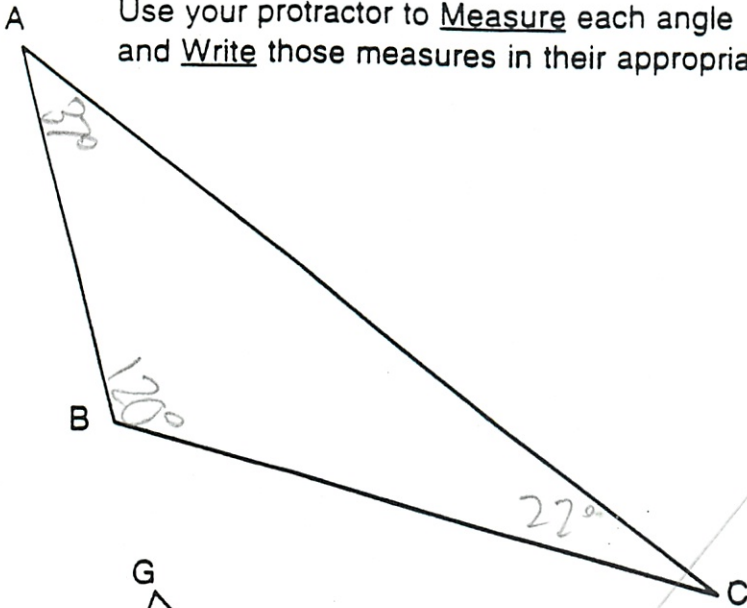
Michael Plasencia

10/20

Degree Discovery

PATTERNS DAY 18

Use your protractor to Measure each angle and Write those measures in their appropriate angles.



$$180(n-2)$$

n = number of sides

Worksheet

Review

Reg Polygon

Angle Sum

Warm Up

$$\begin{aligned}
 & -2^3 - -2^4 + 2 - (-2)^2 - (-1)^3 \\
 & -8 + 16 + 2 - 4 + 1 \\
 & -9 + 22 - \\
 & \textcircled{13} - 12 + 19 \\
 & \textcircled{7}
 \end{aligned}$$

$$-4\frac{1}{2} - -3\frac{1}{3} - 6\frac{1}{8}$$

$$\begin{aligned}
 & -4\frac{12}{24} + 3\frac{8}{24} - 6\frac{3}{24} \\
 & -10\frac{15}{24} + 3\frac{8}{24}
 \end{aligned}$$

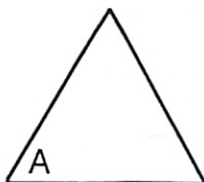
$$\textcircled{-7\frac{7}{24}}$$

$$\begin{array}{r}
 10\frac{15}{24} \\
 3\frac{8}{24} \\
 \hline
 7\frac{7}{24}
 \end{array}$$

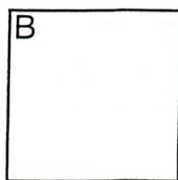
$$180(s/2)/s$$

In each figure, without measuring the angles, calculate the degree measure of each labeled angle. Assume that each figure is regular; that is, that all sides of the figure are the same length and all the angles of the figure have the same measure. In some figures segments are drawn from the center to each vertex.

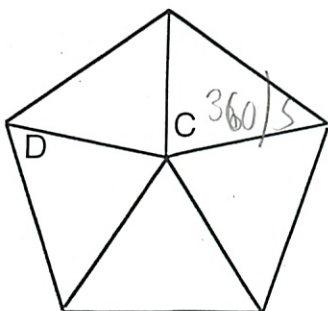
1. Triangle



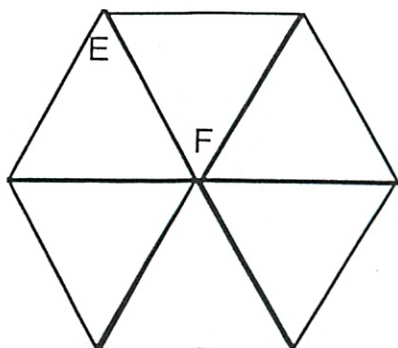
2. Quadrilateral



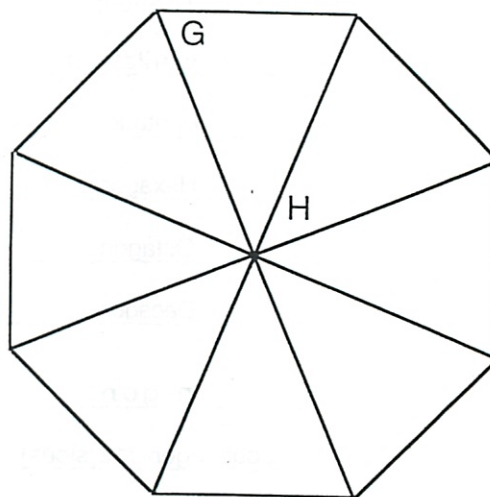
3. Pentagon



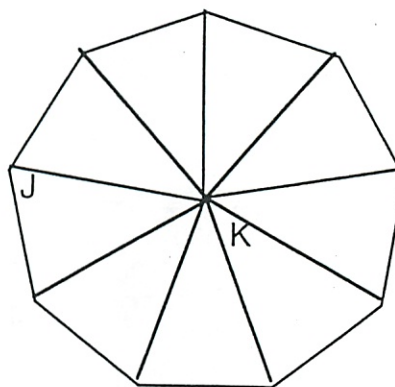
4. Hexagon



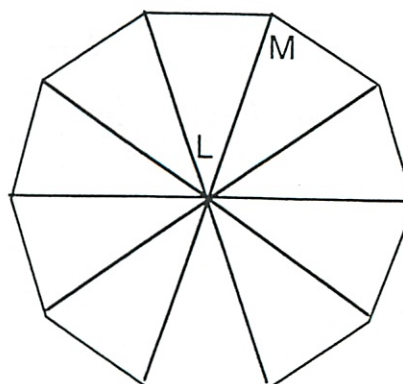
5. Octagon



6. Nonagon



7. Decagon



ANSWERS

$$m\angle A = 60^\circ$$

$$m\angle B = 90^\circ$$

$$m\angle C = 72^\circ$$

$$m\angle D = 108^\circ$$

$$m\angle E = 126^\circ$$

$$m\angle F = 60^\circ$$

$$m\angle G = 135^\circ$$

$$m\angle H = 45^\circ$$

$$m\angle J = 180^\circ$$

$$m\angle K = 40^\circ$$

$$m\angle L = 36^\circ$$

$$m\angle M = 144^\circ$$

x	y
0	4
1	5
2	3
3	4
4	5

Put in order

Fill in so x is continuous

$$180(x-2)$$

Use the information you found about each figure to fill in the following table.

Name of polygon	Measure of one interior angle	Sum of measures of all interior angles
Triangle	60°	180
Quadrilateral	90°	360
Pentagon	108°	540
Hexagon	120°	720
Octagon	135°	1080
Decagon	144°	1440
n-gon	$\frac{180(n-2)}{n}$	$180(n-2)$
dodecagon (12 sides)	150°	1800
20-gon	162°	3240

So its $\frac{x}{2} + 4$

$$y = \frac{x}{2} + 4$$

so its $\frac{1}{2} \times \text{increase} + 4$

$$n^2 + n$$

$$1^2 + 1 + 2^2 + 2 + 3^2 + 3 + \dots + n^2 + n$$

$$2 + 6 + 12 + 20 + 30 + \dots$$

Warm-up 10/22

$$(3)^3 = 9^2$$

$$-27 + 81 = 54$$

$$-4\frac{2}{3} - 5\frac{1}{2} + 2\frac{3}{4}$$

$$-4\frac{2}{3} + 8\frac{1}{4}$$

$$3\frac{1}{3} + 3\frac{7}{12}$$

Have to add -0.7°

$$\frac{1}{4} \quad \frac{1}{2} \quad \frac{1}{4}$$

$$\frac{2}{4} \quad \frac{2}{4} \quad \frac{1}{4}$$

$$-\frac{1}{4}$$

$$-4.9$$

$$-3\frac{1}{2} - 4\frac{1}{3} - 2\frac{3}{8}$$

$$-7\frac{1}{6} - 2\frac{3}{8}$$

$$-10\frac{5}{24}$$

so $4x + 10$ not this

$$32 + 6 + 10 + 14 + 18 + 22 + 26 + 30 + 34$$

$$24 + 30 + 56 + 34$$

$$54 + 90 = 144$$

go back

$$\sum_{x=0}^3 2x^2 - x + 1$$

$$2(0)^2 - 0 + 1 + 2(1)^2 - 1 + 1 + 2(2)^2 - 2 + 1 + 2(3)^2 - 3 + 1$$

$$2(0) + 1 + 2(1) + 2(4) - 1 + 2(8) - 2$$

$$0 + 1 + 2 + 8 - 1 + 18 - 2$$

Patterns 17

Could do this

$$\sum_{x=0}^6 4x + 10$$

$$\sum_{x=2}^8 4x + 2$$

$$\sum_{x=7}^9 x + 3$$

I have trouble doing these (So's)

$$26$$

was correct

Angle

Measure

Quiz

10/18

Pow

#3

Who's Dog?

(P66)

Hobby

10/22

	Dog					Hobby				
	G	J	I	F	H	G	J	I	F	H
Abigail	0	x	x	x	x	x	x	x	0	x
Bertha	x	x	x	x	0	x	x	0	x	x
Candy	x	0	x	x	x	x	x	x	x	0
Dora	x	x	x	0	x	x	x	x	x	x
Eudora	x	x	0	x	x	0	x	x	x	x

	Dog	Hobby
Abigail	George	Frank
Bertha	George	
Candy	Jerry	George
Dora	Frank	
Eudora	Ike	

More than 1 solution because George's Dog is not correctly defined. These husbands can't be found

Futia / Life (P67)

10/25

$\frac{1}{4}$ boy

$\frac{1}{5}$ teen

$\frac{1}{3}$ man

13 old

$\frac{7}{12}$ 35
 $\frac{1}{5}$ 60
 $\frac{12}{60}$

$\frac{42}{60} + 13 = \frac{60}{60} = 1$

- 60 years life living

It's All Gone

p69

$$\begin{array}{r}
 0 \\
 10 \quad \left. \begin{array}{l} +10 \\ \div 2 \end{array} \right\} \\
 5 \quad \left. \begin{array}{l} +10 \\ \div 2 \end{array} \right\} \\
 15 \quad +10 \\
 25 \quad \div 2 \\
 12.5 \quad +10 \\
 8.25 \quad \div 2
 \end{array}$$

Starts w/ 8.25 as he gets double - 17.50 and spends 10. (7.50)
 2nd shop doubles that to 15 and spends 10, to get 5, which is doubled to 10, which he spends and then he is broke

p71 Number Magician

$$\begin{array}{r}
 32 \quad 6 \\
 +8 \quad 21 \\
 40 \quad 63 \\
 \times 3 \quad 354 \\
 120 \quad 18 \\
 +9 \quad -8 \\
 3 \overline{) 129} \quad 10 \\
 \underline{43} \\
 -15 \\
 \hline
 28
 \end{array}$$

1. (28)

$$\begin{array}{r}
 50 \\
 65 \\
 195 \\
 -9 \\
 \hline
 4 \quad 62 \\
 -8
 \end{array}$$

2. The difference is always 4 more than the number called the answer. The Magician just subtracts 4

Here is it simplified

$$x + 15 \times 3 - 9 / 3 - 8$$

$$x + 15 \times 1 - 3 / 1 - 8$$

Simp

$$x + 15 - 3 - 8$$

$$x + 15 - 11$$

$$x + 4$$

(M A Warmup A

Michael Plasencia

10/26

1. $x + 1 + 2 = 12$ $x + 1 + 4 = 17$

~~SP~~ $x + 1 = 10$ ~~SP~~ $x + 1 = 13$

$x = 9$ $x = 12$

(A)

2. $\frac{3}{8}$ participate $\frac{5}{8} = 62.5\%$ dont

$$\begin{array}{r} 12 \\ 125 \\ \times 5 \\ \hline 625 \end{array}$$

(H)

3. $2^n = 128$

$5: 2^4 \times 2^4 \times 2^4 \times 2^4 \times 2^4 = 32$

$6: 32 \times 2 = 64$

$7: 64 \times 2 = 128$

(C)

4. $h - 2 = c$ (J)

$y = 2x + 3$

$+4 \quad 5 = 2(1) + 3$

$+4 \quad 9 = 2(3) + 3$

$13 = 2(5) + 3$

(J)

5. $\frac{2}{6} = \frac{1}{3}$ (C)

7. $12 \quad 23 \quad 34 \quad 45$

$13 \quad 24 \quad 35$

$14 \quad 25$

15

= (10 games)

8. 8 to 12 - 10 to 12 because they show something in relation to the same thing

9.

75

-30

45

-15

30

30

75

6

15

2

5

40

100

(40%)

10. $\frac{1562.5}{8} = 195.3125$ a month $\frac{2232.1428}{7} = 318.8775$

Approx 2232 balls a day

11. 16 (42)

B. $(n-1)^2$ only above 3rd square

C. $(20-1)^2 = 19^2 = 361$
 $19^2 = 361$
 1710
 $\# 1881$

20th Square because I found that $(n-1)^2$ works for squares above 3, when I solved this I found he would have 1881.

How to do double previous (reserving) and put to formula? Need Help!

12. $\frac{500}{214} = 2.336$ $\frac{11}{27} = 0.407$ $\frac{11}{27} = 0.407$

11 more weeks I found

this by first subtracting what she had. I then added $7+20$ to find her weekly income. I then divide

that she needed by the weekly income. I rounded up because she can have more but not less. That was # of weeks remaining

CMA Warmup B

w/ Calculator

10/28

1. $\frac{12}{15} = \frac{4}{5} = 80\%$ (C)

5. $\frac{10}{15} = \frac{2}{3} = 66\%$ (A)

2. (J)

6. (A)

3. $\frac{1}{4} = \frac{25}{100} = 25\%$ (D)

7. 2.50

4. $\frac{2}{24.50}$

5 small + 3 large

$2.5 \times 4 + 4 \times 4 = 2.5 \times 5 + 4 \times 3$

4. (6)

8. $.16, .303, .35, .4, .67$

8b. $\frac{1}{2}, \frac{5}{8}, \frac{3}{4}, \frac{2}{3}, \frac{7}{8}$

We have not learned triangulation

9. A: (2, 5)
B: (2, 0)
C: (2, -3)

10. (8) ?

11. $66\% < x < \frac{4}{5}$

$\frac{4}{5} = .8$

$\frac{17}{20} = 85\%$

$\frac{5}{7} \approx 71\%$

$\frac{9}{25} = 36\%$

A bit more than 66% is between .66 and .8

Quar



16 A

She means that when you multiply 2 multiples of 4 ex. 4×16 the answer is still a multiple of 4

$$4 \cdot 16 = \frac{64}{4}$$

$16 = 50$ multiple

B. Always true because you take a certain # of groups of 4 which still make it a multiple

Quiz

10/25

Unit Test

10/27

Portfolio

Cover +
Letter

(Rough Draft)